

# Globally Polarized Quark-gluon Plasma in Non-central $A + A$ Collisions

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Produced partons have large local relative orbital angular momentum along the direction opposite to the reaction plane in the early stage of non-central heavy-ion collisions. Parton scattering is shown to polarize quarks along the same direction due to spin-orbital coupling. Such global quark polarization will lead to many observable consequences, such as left-right asymmetry of hadron spectra, global transverse polarization of thermal photons, dileptons and hadrons. Hadrons from the decay of polarized resonances will have azimuthal asymmetry similar to the elliptic flow. Global hyperon polarization is studied within different hadronization scenarios and can be easily tested.

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Strong transverse polarization of hyperons has been observed in unpolarized  $p + p$  and  $p + A$  collisions since the 1970's [1]. Given the beam and hyperon momenta  $\vec{p}$  and  $\vec{p}_H$ , hyperons produced in the beam fragmentation region are found transversely polarized in the direction perpendicular to the hyperon production plane,  $\vec{n}_H = \vec{p} \times \vec{p}_H / |\vec{p} \times \vec{p}_H|$ . Polarizations of  $\Lambda$ ,  $\Xi$  and  $\Xi$  are negative while  $\Sigma$  and  $\Sigma$ 's are positive. In the meantime,  $\bar{\Lambda}$  and  $\Omega$  are not transversely polarized. Although the origin for such striking transverse hyperon polarization is still in debate, one can relate it to the single-spin left-right asymmetries observed in hadron-hadron collisions with transversely polarized beam [2], which in turn can be attributed to the orbital angular momenta (o.a.m.) of the valence quarks in a polarized nucleon [3–5], or fragmentation functions of transverse polarized quarks [6] as well as twist-3 parton correlations in nucleons [7]. It was argued [8–11] that the polarization mechanism in  $p+p(A)$  collisions would be absent due to the formation of QGP and therefore hyperon polarization would be diminished in central heavy-ion collisions. However, how QGP destroys the polarization mechanism is yet unclear since one still does not have a satisfactory explanation for the zero polarization for  $\bar{\Lambda}$  and  $\Omega$  in  $p + p(A)$  collisions.

In this Letter, we show that parton interaction in *non-central* heavy-ion collisions leads to a global quark polarization along the opposite direction of the reaction plane,

$$\vec{n}_b = \vec{p} \times \vec{b} / |\vec{p} \times \vec{b}|, \quad (1)$$

as determined by the nuclear impact parameter  $\vec{b}$ . This global polarization is essentially a local manifestation of the global angular momentum of the colliding system through interaction of spin-orbital coupling in QCD. It will have far reaching consequences in non-central heavy-ion collisions, such as left-right asymmetry of hadron spectra in the reaction plane, global transverse polarization of direct photons, dileptons and hadrons with spin. Within different hadronization scenarios, we will discuss hyperon polarization as a result of the global quark polarization. Possible contribution from final state hadronic interaction will also be discussed.

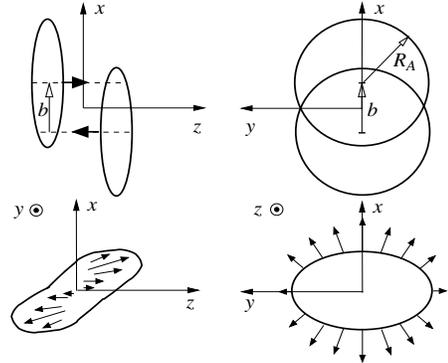


FIG. 1. Illustration of non-central heavy-ion collisions with impact parameter  $\vec{b}$ . The global angular momentum of the produced matter is along  $-\hat{y}$ , opposite to the reaction plane.

Let us consider two colliding nuclei with the beam projectile moving in the direction of the  $z$  axis, as illustrated in Fig. 1. We define the impact parameter  $\vec{b}$  (along  $\hat{x}$ ) as the transverse distance of the projectile from the target nucleus and the reaction plane as given by  $\vec{n}_b$  (along  $\hat{y}$ ) in Eq. (1). Partons produced in the overlapped region of the collision will carry a global angular momentum along the direction opposite to the reaction plane ( $-\hat{y}$ ). A thermalized QGP requires final state parton interaction. Given the nature of partonic interaction at high energy, the global angular momentum would never lead to a collective rotation of the system. It will, however, be manifested in the finite transverse (along  $\hat{x}$ ) gradient of the average longitudinal momentum  $p_z(x, y, b)$  per produced parton. We assume for the moment that  $p_z(x, y, b)$  is independent of the longitudinal position and is just an average value. Given the range of interaction  $\Delta x$ , two colliding partons will have relative longitudinal momentum  $\Delta p_z = \Delta x dp_z / dx$  with o.a.m.  $L_y \sim -\Delta x \Delta p_z$  along the direction of  $\vec{n}_b$ . This relative o.a.m.  $L_y$  will lead to global quark polarization due to spin-orbital coupling.

The initial collective longitudinal momentum can be calculated as the total momentum difference between

participant projectile and target nucleons, whose transverse distributions (integrated over  $y$ ) are,

$$\begin{aligned} \frac{dN_{\text{part}}^{P,T}}{dx} &= \frac{3A}{2\pi R_A} \left\{ \tilde{y}_{\text{max}} \sqrt{1 - \tilde{y}_{\text{max}}^2 - (\tilde{x} \mp \tilde{b}/2)^2} \right. \\ &+ \left. [1 - (\tilde{x} \mp \tilde{b}/2)^2] \arcsin \left[ \frac{\tilde{y}_{\text{max}}}{\sqrt{1 - (\tilde{x} \mp \tilde{b}/2)^2}} \right] \right\}; \\ \tilde{y}_{\text{max}} &= \min \left\{ \sqrt{1 - (\tilde{x} + \tilde{b}/2)^2}, \sqrt{1 - (\tilde{x} - \tilde{b}/2)^2} \right\}, \quad (2) \end{aligned}$$

where  $\tilde{x} = x/R_A$ ,  $\tilde{b} = b/R_A$  and  $R_A = 1.12A^{1/3}$  is the nuclear radius in a hard-sphere distribution.

Since the measured total multiplicity in  $A + A$  collisions is proportional to the number of participant nucleons [12], we can assume the same for the produced partons with a proportionality  $c(s)$ . The average collective longitudinal momentum per parton is then,

$$p_z(x, b) = \left( \frac{\sqrt{s}}{2c(s)} \right) \frac{dN_{\text{part}}^P/dx - dN_{\text{part}}^T/dx}{dN_{\text{part}}^P/dx + dN_{\text{part}}^T/dx}. \quad (3)$$

The distribution  $p_z(x, b)$  is an odd function in both  $x$  and  $b$  and therefore vanishes at  $x = 0$  or  $b = 0$ . As shown in Fig. 2 (as dashed lines) in units of  $4p_0 \equiv 4\sqrt{s}/2c(s)$  and as a function of  $\tilde{x}$  for different values of  $\tilde{b}$ , it is a monotonically increasing function of  $\tilde{x}$  until the edge of the overlapped region  $|\tilde{x} \pm \tilde{b}/2| = 1$  where it drops to zero. The transverse gradient  $dp_z/dx$ , shown as solid lines in unit of  $dp_0/dx \equiv \sqrt{s}/2c(s)R_A$ , is an even function of  $x$  and vanishes at  $b = 0$ . It increases almost linearly with  $b$  for small and intermediate values of  $b$ . Except the singular behavior at the boundary of the overlapped region which is caused by the assumed hard-sphere nuclear distribution,  $dp_z/dx$  is approximately uniform across the transverse  $x$ -direction. The classical relative o.a.m. is then  $L_y \equiv -(\Delta x)^2 dp_z/dx$  for partons separated by  $\Delta x$  in the transverse direction. Due to transverse expansion,  $dp_z/dx$  will decrease with time according to  $(R_A - b/2)/[R_A - b/2 + v_x(b)(\tau - \tau_0)]$ , where  $v_x(b)$  is the transverse flow velocity in the reaction plane.

In  $Au + Au$  collisions at  $\sqrt{s} = 200$  GeV, the number of charged hadrons per participant nucleon is about 15 [12]. Assuming the number of partons per (meson dominated) hadron is about 2, then  $c(s) \simeq 45$ . Given  $R_A = 6.5$  fm,  $dp_0/dx \simeq 0.34$  GeV/fm and  $L_0 \equiv -(\Delta x)^2 dp_0/dx \simeq 1.7$  for  $\Delta x = 1$  fm.

We can relax the approximation of uniform distribution of  $p_z(x, b)$  in the longitudinal direction by identifying pseudo-rapidity with the spatial rapidity  $\eta = 0.5 \ln(t + z)/(t - z)$ . According to experimental studies of hadron production in  $p + A$  and  $A + B$  collisions, the collective longitudinal momentum  $p_z$  and  $dp_z/dx$  are distributed across a broad range of rapidity and peaks in the forward (backward) region for a given layer of dense matter at positive (negative)  $x$ . The position of the peak in rapidity should increase with  $|x|$ . Note that even though  $p_z(x, b)$  vanishes at around  $x = 0$ ,  $dp_z/dx$  and  $L_y$  are

still finite for  $b \neq 0$  as shown in Fig. 2. Averaging over the  $x$ -direction will result in finite  $dp_z/dx$  and  $L_y$  around central rapidity region in non-central heavy-ion collisions.

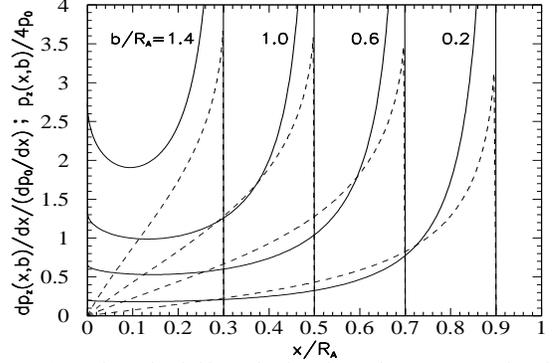


FIG. 2.  $(dp_z/dx)/(dp_0/dx)$  (solid) and  $p_z(x, b)/4p_0$  (dashed) as functions of  $x/R_A$  for different values of  $b/R_A$ .

To study quark polarization due to parton collisions with a fixed direction of o.a.m., we consider quark scattering with fixed impact parameter  $\vec{x}_T$ . For given initial relative momentum  $(E, \vec{p})$  and final spin  $\lambda/2$  of the quark along  $\vec{n}_b$ , the cross section is,

$$\begin{aligned} \frac{d\sigma_\lambda}{d^2x_T} &= C_T \int \frac{d^2q_T}{(2\pi)^2} \frac{d^2k_T}{(2\pi)^2} e^{i(\vec{k}_T - \vec{q}_T) \cdot \vec{x}_T} \mathcal{I}_\lambda(\vec{q}_T, \vec{k}_T, E), \\ \mathcal{I}_\lambda &= \frac{g^2}{2(2E)^2} \bar{u}_\lambda(p_q) A(\vec{q}_T) (\not{p} + m_q) A(\vec{k}_T) u_\lambda(p_k), \quad (4) \end{aligned}$$

within the screened potential model [13], where  $A_0(q_T) = g/(q_T^2 + \mu^2)$  is the screened static potential with Debye screen mass  $\mu$ ,  $C_T$  is the color factor associated with the target. Average over spin polarization is implied for the initial quark and  $\vec{p}_{q(k)} = \vec{p} + \vec{q}_T(\vec{k}_T)$  is the final quark momentum. For small angle scattering,  $q_T, k_T \sim \mu \ll E$ ,

$$\frac{\mathcal{I}_\lambda}{g^2} \approx \frac{1}{2} A_0(q_T) A_0(k_T) \left[ 1 - i\lambda \frac{(\vec{q}_T - \vec{k}_T) \cdot (\vec{n}_b \times \vec{p})}{2E(E + m_q)} \right]. \quad (5)$$

The first term gives the unpolarized cross section

$$\frac{d\sigma}{d^2x_T} \equiv \frac{d\sigma_+}{d^2x_T} + \frac{d\sigma_-}{d^2x_T} = 4C_T \alpha_s^2 K_0^2(\mu x_T), \quad (6)$$

or  $d\sigma/dq_T^2 = C_T 4\pi \alpha_s^2 / (q_T^2 + \mu^2)^2$  in momentum space. The second term gives rise to a polarized cross section  $d\Delta\sigma/d^2x_T \equiv d\sigma_+/d^2x_T - d\sigma_-/d^2x_T$ ,

$$\frac{d\Delta\sigma}{d^2x_T} = -\mu \frac{\vec{p} \cdot (\hat{x}_T \times \vec{n}_b)}{E(E + m_q)} 4C_T \alpha_s^2 K_0(\mu x_T) K_1(\mu x_T), \quad (7)$$

where  $\hat{x}_T = \vec{x}_T/x_T$  and  $K_n$ 's are modified Bessel functions. It is evident that parton scattering polarizes quarks along the direction opposite to the parton reaction plane determined by the impact parameter  $\vec{x}_T$ , the same direction of the relative o.a.m. This is essentially

the manifest of spin-orbital coupling in QCD. Ordinarily, the polarized cross section along a fixed direction  $\vec{n}_b$  vanishes when averaged over all possible direction of the parton impact parameter  $\vec{x}_T$ . However, in non-central heavy-ion collisions the local relative o.a.m.  $L_y$  provides a preferred average reaction plane for parton collisions. This will lead to a global quark polarization opposite to the reaction plane of nucleus-nucleus collisions. This conclusion should not depend on our perturbative treatment of parton scattering as far as the effective interaction is mediated by the vector coupling in QCD.

Averaging over the relative angle between parton  $\vec{x}_T$  and nuclear impact parameter  $\vec{b}$  from  $-\pi/2$  to  $\pi/2$  and over  $x_T$ , one can obtain the global quark polarization,

$$P_q = -\pi\mu p/4E(E + m_q) \quad (8)$$

via a single scattering for given  $E$ . If we take  $p = \Delta p_z/2 = \vec{x}_T \cdot \hat{x} dp_z/dx$  before averaging, the result will be similar but numerical evaluation is needed. In the limit  $m_q = 0$  and  $p \ll \mu$ , one expects  $P_q \sim -\Delta p_z/\mu$ . Given an average range of interaction  $\Delta x^{-1} \sim \mu \sim 0.5$  GeV and  $dp_0/dx = 0.34$  GeV/fm for semi-peripheral ( $b = R_A$ ) collisions (see Fig. 2) at RHIC,  $P_q \sim -0.3$ . Multiple scattering will further increase the polarization.

In nonrelativistic limit for massive quarks,  $m_q \gg p, \mu$ ,

$$P_q \approx -\pi\mu p/8m_q^2. \quad (9)$$

In the same limit, the spin-orbital coupling energy is  $E_{LS} = (\vec{L} \cdot \vec{S})(dV_0/dr)/(r m_q^2)$ . Given the range of interaction  $r \sim 1/\mu$ ,  $dV_0/dr \sim -\mu^2$  and  $L \sim p/\mu$ ,  $E_{LS}/\mu \sim -\mu p/m_q^2$  is just the above quark polarization.

The global quark polarization opposite to the reaction plane will have many observable consequences in non-central heavy-ion collisions if an interacting QGP is formed. One expects to see left-right asymmetry in hadron spectra at large rapidity similar to the single-spin asymmetry in  $p + p$  collisions [3–7]. Thermal photons, dileptons and final hadrons with spin will be similarly polarized. Since hadrons from the strong decay of polarized resonances have angular distributions that prefer the direction perpendicular to the resonances' polarization, they will result in an azimuthal asymmetry with respect to the reaction plane, similar to the asymmetry due to elliptic flow. In the following, we will discuss global hyperon polarization since it can be easily measured through the weak decay.

To demonstrate the robustness of the qualitative features of the predicted hyperon polarization due to global quark polarization, we consider several hadronization scenarios. We consider first hadronization via parton recombination. In this case, not only the spin of polarized quarks but also the relative o.a.m. can contribute to the final hadrons' polarization. Given hadron size  $\Delta x$ , the classical estimate of the relative o.a.m. is  $L_y \sim -(\Delta x)^2 dp_z/dx$ . In the nonrelativistic quark model, however, constituent quarks in the ground state are all in

the s-wave state. The contribution of o.a.m. to hadron polarization resides in the o.a.m. of the current valence quark of each constituent quark.

The average o.a.m. of the valence quark can be estimated in a relativistic quark model in a central confining well with a radius  $R$ . It is known that o.a.m. is *not* a good quantum number for a relativistic Dirac particle confined in a limited space, independent of the details of the confining system. The eigenstates can only be characterized by the total angular momentum  $\vec{j} = \vec{l} + \vec{s}$ . Hence, o.a.m. is always involved for massless quarks even when they are in their ground states.

For the ground state  $j = 1/2, j_z = 1/2$  and parity  $\mathcal{P} = +$ , the average o.a.m. is [4],

$$\langle \hat{l}_z(\varepsilon_0) \rangle = \frac{2}{3} \int_0^R g_{01}^2(r) r^2 dr, \quad (10)$$

with  $g_{01}(r) = N[\cos(\varepsilon_0 r)/\varepsilon_0 r - \sin(\varepsilon_0 r)/(\varepsilon_0 r)^2]$ , where  $\varepsilon_0 = M_q$  is the constituent quark mass and  $N$  is a normalization constant. By fixing  $R$  with  $3\varepsilon_0 = M_p$ , we obtain  $2\langle l_z \rangle \approx 0.36$ . This implies that about 30% of the total angular momentum of a constituent quark originates from the o.a.m. of the valence quark. This can be considered as an estimate of the maximal contribution to the constituent quark polarization from the local o.a.m. Over all, the effective polarization of a constituent quark should be proportional to that of the valence quark. Alternatively, polarization of constituent quarks can also be similarly estimated, *e.g.* Eq. (9), assuming massive constituent quarks as point-like particles.

We can categorize recombination into exclusive  $q_\uparrow q_\uparrow q_\uparrow \rightarrow H_\uparrow$  and inclusive  $q_\uparrow q_\uparrow q_\uparrow \rightarrow H_\uparrow + X$  processes. Given baryons' SU(6) wavefunctions in the quark model, the polarization for strange ( $P_s$ ) and non-strange quark ( $P_q$ ), one can obtain the hyperon polarization and recombination probability from the exclusive recombination,  $P_\Lambda = P_s, R_\Lambda = 3(1 - P_q^2)$ ;  $P_\Omega = 2P_s(5 + P_s^2)/R_\Omega, R_\Omega = 6(1 + P_s^2)$ ;

$$P_\Sigma = (4P_q - P_s - 3P_s P_q^2)/R_\Sigma, \quad R_\Sigma = 3 - 4P_q P_s + P_q^2;$$

$$P_\Xi = (4P_s - P_q - 3P_q P_s^2)/R_\Xi, \quad R_\Xi = 3 - 4P_q P_s + P_s^2.$$

If  $P_s \simeq P_q$  in the most likely case, we have the same  $P_H = P_q$  with  $R_H = 3(1 - P_q^2)$  for  $\Lambda, \Sigma$  and  $\Xi$ .

It is difficult to estimate hyperon polarization from inclusive recombination. However, one expects that it is the dominant process for the bulk hadron production, especially for large values of  $P_q$ . It is also required by entropy conservation. The polarization of produced hyperons would be smaller than in the exclusive recombination but should be proportional to  $P_q$ .

The extreme limit of inclusive recombination is fragmentation of polarized quarks,  $q_\uparrow \rightarrow H_\uparrow + X$ . Longitudinal polarization of hyperons in a similar process  $e^+ e^- \rightarrow Z^0 \rightarrow q\bar{q} \rightarrow \Lambda + X$  has been measured [14] and can be explained [15] by assuming that polarized hyperons contain the initial polarized leading quark in its

SU(6) wavefunction. One can similarly calculate hyperon polarization from fragmentation of transversely polarized quarks and obtain,

$$P_\Lambda = n_s P_s / (n_s + 2f_s), P_\Sigma = (4f_s P_q - n_s P_s) / 3(2f_s + n_s), \\ P_\Xi = (4n_s P_s - f_s P_q) / 3(2n_s + f_s), P_\Omega = P_s / 3,$$

where  $n_s$  and  $f_s$  are the strange quark abundances relative to up or down quarks in QGP and quark fragmentation, respectively. Including production of unpolarized hyperons in the process, the effective hyperon polarization from fragmentation of polarized quarks should increase with the fractional momentum  $z_H = p_H / p_q$ .

Because of the complication from hadronization, we cannot quantitatively estimate the final hyperon polarization. We can nevertheless provide qualitative predictions of the global hyperon polarization  $P_H$  in non-central heavy-ion collisions: (1) Hyperons and their anti-particles are similarly polarized along the same direction perpendicular to the reaction plane in non-central heavy-ion collisions. (2) The global hyperon polarization  $P_H$  vanishes in central collisions and increases almost linearly with  $b$  in semi-central collisions. (3) It should have a finite value at small  $p_T$  and in the central rapidity region. It should increase with rapidity and eventually decreases and vanishes at large rapidities. (4) High  $p_T \gg \Delta p_z \sim \mu L_0$  quarks should not be polarized by parton scattering in the medium. However, hyperon polarization should persist at moderate  $p_T$  where recombination of unpolarized high  $p_T$  quarks with polarized thermal quarks may still dominate. The polarization can be estimated within a recombination model. (5) Since hyperon's production planes are randomly oriented with respect to the reaction plane of heavy-ion collisions, the observed hyperon polarization in  $p + A$  collisions should not contribute to the global polarization as we have defined here, except at large rapidity region where directed flow is observed [16]. In this region, the non-vanishing  $\langle p_x \rangle$  can provide an average production plane  $\vec{n}_H$  for hyperons. According to the observed polarization pattern in  $p + A$  [1], the global  $P_H$  will be enhanced for  $\Lambda$ ,  $\Xi$ , and  $\bar{\Xi}$  and reduced for  $\Sigma$  in large rapidity region. In addition, one also expects  $P_\Lambda > P_{\bar{\Lambda}}$  due to the directed flow.

Additional contributions can also arise from hadronic interaction with a given direction of relative o.a.m., since it can also lead to hyperon polarization perpendicular to the reaction plane. Neglecting hyperon production in the hadronic phase, the dominant hadronic processes involving hyperons will be hyperon- $\pi$  scattering, whose amplitude in general has the form [17]

$$M_{\pi H} = \bar{u}(p_f) [S(E, q) + \frac{1}{2}(\not{k} + \not{k}_f)V(E, q)]u(p). \quad (11)$$

One can show that global hyperon polarization from the second term is along while polarizations from the first term and all the interferences are against the global quark polarization. Therefore, polarizations from different channels in hyperon- $\pi$  scattering partially cancel each

other. In addition, the transverse gradient of the longitudinal flow should be significantly reduced in the hadronic phase due to prior strong transverse expansion in the reaction plane as demonstrated by the large elliptic flow measured at RHIC. Therefore, the net effect of hadronic interaction should be small and should not change the final hyperon polarization significantly, in particular at large  $p_T$ . We will leave detailed study to future work.

In summary, produced partons are shown to have large local relative o.a.m. in non-central heavy-ion collisions if quark-gluon plasma is formed. Parton scattering with given relative o.a.m. is shown to polarize quarks along the same direction due to spin-orbital coupling. Such global quark polarization has many measurable consequences in high-energy heavy-ion collisions. Within different hadronization scenarios, we predict that hyperons will be polarized along the opposite direction of the reaction plane. Effects of hadronic interaction are expected to be small and would not change the qualitative feature of our prediction.

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