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INTERPRETATION OF EXPERIMENTS ON THE PHOTO-NUCLEAR EFFECT IN HEAVY ELEMENTS

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November 30, 1951

Berkeley, California

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ABSTRACT

An analysis of the experiments to date on photo-nuclear reactions in heavy nuclei leads to the following results. There is a correlation between the energy at which the (γ, n) cross section is a maximum and the (γ, 2n) threshold. The shape of the total photon absorption cross sections in Sb and Ta can be estimated up to 22 Mev and there is an indication that the cross section drops off strongly above that energy. Using the estimate of the shape of the total cross section in Ta, one can calculate the neutron yield to be expected in experiments with 330 Mev-bremsstrahlung. The calculated value is only about 60% of the experimental value. Evidence is presented that the discrepancy is due to neutrons produced by high energy photons, presumably due to mesonic effects. The integrated cross sections for Zn^{64}, Sb and Ta^{173} can be evaluated and by comparison with the Levinger-Bethe formula lead to values of 0.56, $>$ .44 and 0.50, respectively, for the fraction of exchange force in the neutron-proton interaction, assuming that all of the photo-effect is due to electric dipole transitions.

INTERPRETATION OF EXPERIMENTS ON THE PHOTO-NUCLEAR EFFECT IN HEAVY ELEMENTS

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November 30, 1951

I. Introduction.

There have been many experiments on the photo-nuclear effect[1-39]. Some of these

1. G. C. Baldwin and G. S. Kaiber, Phys. Rev. 70, 259 (1946).
2. O. Hirzel and H. Waffler, Helv. Phys. Acta. ~~19~~ 20, 373 (1947).
3. J. L. Lawson and M. L. Perlman, Phys. Rev. 74, 1190 (1948).
4. M. L. Perlman and G. Friedlander, Phys. Rev. 74, 445 (1948) and M. L. Perlman, Phys. Rev. 75, 988 (1949).
5. H. Waffler and O. Hirzel, Helv. Phys. Acta. 21, 200 (1948).
6. N. W. Curtis, et al., Phys. Rev. 77, 290 (1950).
7. E. R. Gaerttner and M. L. Yeater, Phys. Rev. 77, 714 (1950) and E. R. Gaerttner and M. L. Yeater, Phys. Rev. 77, 570 (1950).
8. G. A. Price and D. W. Kerst, Phys. Rev. 77, 806 (1950).
9. H. L. Poss, Phys. Rev. 79, 539 (1950).
10. D. W. Kerst and G. A. Price, Phys. Rev. 79, 725 (1950).
11. B. C. Diven and G. M. Almy, Phys. Rev. 80, 407 (1950).
12. A. K. Mann and J. Halpern, Phys. Rev. 80, 470 (1950).
13. Seishi Kikuchi, Phys. Rev. 80, 492 (1950).
14. B. D. McDaniel, R. L. Walker, and M. B. Stearns, Phys. Rev. 80, 807 (1950).
15. H. E. Johns, et al., Phys. Rev. 80, 1062 (1950).
16. Byerly and Stephens, Phys. Rev. 81, 473 (1951).
17. R. N. H. Haslam and H. M. Skarsgard, Phys. Rev. 81, 479 (1951).
18. L. Katz and A. S. Penfold, Phys. Rev. 81, 815 (1951).
19. L. Katz and A. S. Penfold, Phys. Rev. 83, 169 (1951).

20. N. Sugarman and R. Peters, Phys. Rev. 81, 951 (1951).

21. Karl Strauch, Phys. Rev. 81, 973 (1951).

22. Seishi Kikuchi, Phys. Rev. 81, 1060 (1951).

23. Richard D. Miller, Phys. Rev. 82, 260 (1951).

24. R. N. H. Haslam, H. E. Johns, and R. J. Horsley, Phys. Rev. 82, 270 (1951).

25. L. Katz, et al., Phys. Rev. 82, 271 (1951).

26. E. R. Gaerttner and M. L. Yeater, Phys. Rev. 82, 461 (1951).

27. W. E. Stephens, J. Halpern, and R. Sher, Phys. Rev. 82, 511 (1951).

28. M. Elaine Toms and William E. Stephens, Phys. Rev. 82, 709 (1951).

29. A. K. Mann and J. Halpern, Phys. Rev. 82, 733 (1951).

30. K. M. Terwilliger, L. W. Jones, and W. N. Jarmie, Phys. Rev. 82, 820 (1951).

31. C. Levinthal and A. Silverman, Phys. Rev. 82, 822 (1951).

32. P. R. Byerly, Jr. and W. E. Stephens, Phys. Rev. 83, 54 (1951).

33. E. R. Gaerttner and M. L. Yeater, Phys. Rev. 83, 146 (1951).

34. R. Sagane, Phys. Rev. 83, 174 (1951).

35. L. Marshall, A. H. Rosenfeld, and S. C. Wright, Phys. Rev. 83, 305 (1951).

36. L. Lundby and L. Marshall, Phys. Rev. 83, 323 (1951).

37. L. Marshall, Phys. Rev. 83, 345 (1951).

38. J. Halpern and A. K. Mann, Phys. Rev. 83, 370 (1951).

39. D. H. Wilkinson and J. H. Carver, Phys. Rev. 83, 466 (1951).

have been interpreted as agreeing with Bohr's model of the compound nucleus, whereas others have seemed to disagree. Thus, Hirzel and Wäffler[2] measured the ratio of emitted protons to neutrons from nuclei irradiated by 17.5 Mev γ-rays and found that this ratio was

much higher than that predicted by compound nucleus theory. Another apparent discrepancy arose when it was established that the (γ, n) cross section in medium weight elements had a maximum around 20 Mev and dropped off sharply for higher energies. According to compound nucleus theory, this drop-off should be due to the competition to the (γ, n) reaction afforded by the (γ, 2n). But experimentally, it appeared that the (γ, 2n) cross section was much too small to furnish appreciable competition. It was this discrepancy, among others, that led Goldhaber and Teller[40] to propose their special model of nuclear dipole vibrations. Finally, various observers have found that the angular distribution of high energy protons from (γ, p) reactions is not spherically symmetrical, in contradiction to the predictions of the compound nucleus.

On the other hand, there were experiments which were in good agreement with compound nucleus theory. Thus, the angular distribution of the low energy neutrons and protons produced in the nuclear photoeffect was measured by various workers and found to be spherically symmetrical[10,11,30]. Also, the energy distribution of the neutrons and protons was in good agreement with the compound nucleus model[11]. Moreover, Byerly and Stephens[16] measured the ratio of neutrons to protons emitted from Cu when irradiated with 24 Mev-bremsstrahlung and found excellent agreement with the predictions of Weisskopf and Ewing[41], which were based on the compound nucleus model.

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[40] M. Goldhaber and E. Teller, Phys. Rev. 74, 1046 (1948).

[41] V. Weisskopf and D. H. Ewing, Phys. Rev. 57, 472 (1940).

These apparently contradictory results are, we think, resolved in part by the suggestion of Courant[42] that there may be a direct photo-effect on protons, in which they are ejected from the nucleus without a compound nucleus being formed. The cross section for this process can be quite small and still explain the anomalously large number of protons in Hirzel and Wäffler's experiment. Also, this hypothesis explains naturally the angular asymmetry of high energy protons mentioned above. Moreover, it does not destroy the agreement with the compound nucleus theory that Byerly and Stephens found. The directly-ejected protons are important only when the proton binding energy is so high that the number of evaporated protons is small. This is the case in the experiments of Hirzel and Waffler but is not so for Cu^{63}, the element measured by Byerly and Stephens.

There is also no contradiction between compound nucleus theory and the fact mentioned above, that the (γ, 2n) cross section in Cu^{63} is much too small to provide competition for the (γ, n) reaction. It appears experimentally that the (γ, np) cross section is much larger than the (γ, 2n) cross section and, indeed, sufficiently large to afford competition.

There is some other evidence that has not been presented before for the validity of the statistical model. For heavy nuclei, the emission of a proton is strongly inhibited by the

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[42] E. Courant, Phys. Rev. 82, 703 (1951).

coulomb barrier. The only important processes appear to be the emission of neutrons. If the statistical theory and the idea of competition is correct, we would expect to find a correlation between the energy at which the (γ, n) cross section is maximum and the threshold of the (γ, 2n) reaction. Evidence for such a correlation is presented in Section III.

The statistical model predicts what happens after the nucleus absorbs a photon. There are also theories which say something about the absorption of the photon in the first place. In particular, we shall consider the work of Levinger and Bethe[43]. Using so-called 'sum rules' these authors calculate the integrated cross section for dipole absorption of a photon. They get the formula

$$\int_0^\infty \sigma_{total}(W)\, dW = .060 \frac{NZ}{A} (1 + 0.8x) \qquad (1)$$

Here x is the fraction of exchange force in the neutron-proton potential (assumed to be due to central forces only). $\sigma_{total}(W)$ is the sum of all processes in which a photon is absorbed, i.e., it is the sum of the cross sections for all such processes as (γ, n), (γ, p), (γ, 2n), etc. If we have an experimental value for this sum, we have a means of deducing the fraction of exchange force in the neutron-proton potential, always remembering

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43 J. S. Levinger and H. A. Bethe, Phys. Rev. 78, 115 (1950).

the assumption of dipole transition. The integral in Eq. (1) can be evaluated from the available data in some cases. This is discussed in Section VI.

The experiments that we have analyzed to obtain the results stated above have been of two major kinds. The first kind is that in which the integrated cross section and sometimes the detailed shape of a particular reaction is measured, detecting the reaction by the method of induced radioactivity. The second kind is that in which the total neutron yield is measured from a target irradiated by bremsstrahlung or some other source of photons. The latter method has the advantage that one gets information about all reactions in which a neutron is emitted, but it has the corresponding disadvantage that one cannot immediately isolate the contribution to the total cross section from particular reactions. This disadvantage can be overcome to some extent by comparing the results of experiments done at different maximum bremsstrahlung energies. Among the experiments which we shall use, are that of McDaniel, et al.[14] on neutron yields using photons from the Li(p, γ) reaction, that of Price and Kerst[8] using bremmsstrahlung at 18 and 22 Mev maximum energy and those of Terwilliger, et al.[30] and of Kerst[10] using bremsstrahlung at about 330 Mev maximum energy. By comparing the difference between the 18 and 22 Mev yields, one gets information about the cross section for neutron emission between these energies; this is mainly information about the (γ, 2n) cross section for heavy elements. By further comparing the 22 Mev results

with the 330 Mev results, we can find something about the contribution of the cross section between 22 and 330 Mev.

In the next section, we present a compilation of the data on individual reactions and in the following section, show that for heavy elements there is a strong correlation between the (γ, 2n) threshold and the peak of the (γ, n) cross section. In Section IV, we try to estimate the magnitude of the (γ, 2n) cross section in some elements by comparing the 18 and 22 Mev data of Kerst and Price and by using the results of McDaniel mentioned above. We can then use this estimate and the 330 Mev bremsstrahlung data to try to find something about the cross section between 22 and 330 Mev. This work, plus other evidence presented in Section V, indicates that the total cross section drops off quite sharply above 22 Mev and begins to rise again at energies of the order of 200 Mev. This rise may be due to mesonic effects. In Section VI, we use our deductions from the experimental data to calculate the integrated cross section and hence, the fraction of exchange force in the n-p interaction.

II. Summary of Data

In Table I we present a summary of the data available on photo-nuclear reactions. There are some interesting features to note in this table. The first is the rather regular rise of the integrated cross section for (γ, n) reactions. Also, there is a slight indication that for elements heavier than Cu, the (γ, n) half-width decreases slowly with Z. As opposed to the (γ, n) reactions, the integrated cross section for (γ, p) reactions rises

with Z up to about Z = 28 and then begins to drop off. This trend is confirmed by the work of Mann and Halpern[29], who measure the yields of (γ, p) reactions as a function of Z. These yields are roughly proportional to the integrated cross section. Mann and Halpern also find a maximum yield at around Z = 30. At this point the yields are of the same order of magnitude as for the (γ, n) reaction. Beyond Z = 30, however, the proton yield drops off rapidly and at Z = 50 is about one-hundredth the neutron yield. This is easily understandable as due to the effect of the coulomb barrier. It suggests that in heavy elements one can confine attention to processes in which a neutron is emitted. The last point to be noted in Table I is that the integrated cross section for the (γ, pn) reaction in a medium weight element can be much larger than that for the (γ, 2n) reaction. For $^{30}Zn^{64}$, e.g., the integrated (γ, pn) cross section is about 0.4 of the integrated (γ, n) cross section. This suggests that, if the statistical model holds, competition in medium weight elements may be provided by (γ, pn) rather than (γ, 2n) reactions.

Table I. Summary of data on photo-nuclear reactions.

(γ, n) reactions

Isotope	Threshold	W_{max}	Half-Width	$\int \sigma dW$ (Mev-barns)	Reference
C^{12}	18.7	22.4		0.047	24
C^{12}				0.086	35
C^{12}				0.107	21
Al^{27}	14	19.6			
P^{31}	12.4	19.0	7.5	.120	18
Fe^{54}	18.3		5.7	0.42	25
Ni^{58}	18.5		4.6	0.33	25
Cu^{63}	10.9	17.5	6.0	0.70	15
Cu^{63}	10.9			0.77 ± 0.15	35
Cu^{63}	10.9	17.5		0.60	11
Cu^{65}	10.2	19.0	6.0	1.40	15
Cu^{65}		19.0		0.89	21*
Zn^{64}	19.0			0.61	21*
Zn^{64}	18.5		7.1	0.83	25
Zn^{64}				0.77	35
Ag^{109}		16.5		1.65	11
Sb^{121}	9.3	14.5	5.5	>1.2	15
Sb^{123}	9.3	14.5	5.5	2.0	15
Ta^{181}	8.0	13.5	4.5	>0.39	15

(Continued)

Table I. (Cont.)

Isotope	Threshold	W_{max}	Half-Width	$\int \sigma dW$ (Mev-barns)	Reference
		(γ, p) reactions			
C^{12}		21.5 ± 0.5	1.7	0.063 ± 0.016	38
Mg^{25}		21		0.056 ± 0.03	28
Al^{29}		21.2 ± 0.5	5.4	0.12 ± 0.03	38
Ni {67% Ni^{58}, 27% Ni^{60}}		18.7	5.4	0.32 ± 0.08	38
$^{27}Co^{52}$		21.5	5.7	0.14 ± 0.04	38
$^{30}Zn^{68}$				0.068	21
$^{41}Cb^{93}$		21.3	6.6	0.12 ± 0.03	38
		Higher order reactions			
Reaction					
$S^{32}(\gamma, np+d)$				.004	18
$Zn^{64}(\gamma, pn)Cu^{62}$				.26	21*
$Zn^{66}(\gamma, pn)Cu^{64}$				.13	21*
$Zn^{64}(\gamma, 2n)Cu^{62}$				.047	21*
$Cu^{63}(\gamma, 2n)Cu^{61}$				.035	34*

* In this reference the measurements of integrated cross-sections are relative to that of Cu^{63}. To convert these relative values to the absolute ones given in this table we have taken as the integrated cross-section for Cu^{63} the mean of the three values given above, i.e., 0.69 Mev-barns.

III. Correlation between Energy at which (γ, n) Cross Section Is Maximum and Threshold of the (γ, 2n) Reaction.

According to the Bohr concept of the compound nucleus, the cross section $\sigma_{\gamma,a}(W)$ for a reaction in which a particle a* is emitted when a photon of energy W is incident on a nucleus, is $\sigma_{\gamma,a}(W) = \sigma_{abs.}(W) \times P_a(W)$. Here $\sigma_{abs.}(W)$ is the cross section for absorption of a photon of energy W, and $P_a(W)$ is the probability that at excitation energy W, the nucleus emits a particle of type a. Now, as is well-known, the cross section of the (γ, n) reaction, $\sigma_{\gamma,n}(W)$, has a maximum around 19 Mev for medium weight elements and at somewhat smaller values for heavier elements. In all measured cases, the cross section is small or zero near threshold and rises sharply to the maximum. We will say nothing about this initial rise here. A maximum in the (γ, n) absorption cross section could be caused by a maximum in $\sigma_{abs.}(W)$, or, if we assume that $\sigma_{abs.}(W)$ is more or less flat near W_m, the maximum could be caused by a dropping off of $P_a(W)$. The last assumption seems to us to be much less restrictive.

If we make it, we would expect to find a correlation in heavy elements between the energy W_m at which the (γ, n) cross section is maximum and the (γ, 2n) threshold. We have restricted this statement to heavy elements because, as we have discussed

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* We shall let the subscript a signify several particles if the excitation energy W is high enough that they can be emitted.

in the introduction, it is only for these that one can be reasonably certain a priori, that essentially only neutrons are emitted. For medium weight elements, we would expect a correlation if the (γ, 2n) process dominated the (γ, pn). We are reasonably sure that this is the case for Cu^{65}, for which Byerly and Stephens have found that proton emission is small compared with neutron emission. Thus, we include Cu^{65} along with four other heavy elements in Table II, which seems to show that there is a real correlation between W_m and the (γ, 2n) threshold.

Table II. Comparison of the (γ, 2n) threshold and energy W_m at which the (γ, n) cross section is maximum.

Element	W_m	(γ, 2n) threshold
$^{29}Cu^{65}$	19.0	18.1
$^{47}Ag^{109}$	16.5	16.05 ± .28
$^{51}Sb^{121}$	14.5	15.6 ± .3
$^{51}Sb^{123}$	14.5	15.4
$^{73}Ta^{181}$	14.0*	14.1

* This value is a later one than that presented in Table I and is taken from a preprint of a paper by R. N. H. Haslam, L. A. Smith, and J. G. V. Taylor.

A word about the method of calculating the (γ, 2n) thresholds given in the third column of Table II may be useful here. That for Ag^{109} is obtained by adding the value given by Sher, et al.[44] for the photo-neutron threshold in Ag^{109} to Harvey's[45] value for the photo-neutron threshold in Ag^{108}. Similarly, for Sb^{123} we have used Sher's value for the threshold in Sb^{123} and Harvey's for the threshold in Sb^{121}. For the other elements, we have had to add the measured values of the (γ, n) threshold (from Harvey and/or Sher) in the original nucleus and the value calculated from the semi-empirical mass formula for the final nucleus, or vice-versa. The measured values have probable errors of about 0.2 Mev. A comparison of Harvey's data on some neighboring elements with the calculated values for those elements, indicates that the calculated values that enter here should be good to within 0.3 or 0.4 Mev. Therefore, we expect the (γ, 2n) thresholds given in Table II for Cu, Sb^{123} and Ta to be accurate to perhaps 0.5 Mev. Probably, this is the magnitude of error in the position in the maximum of the cross section. Thus, our values seem to be sufficiently accurate as not to destroy the correlation, if there is one.

IV. Estimate of (γ, n) and (γ, 2n) Cross Section for Sb and Ta.

In this section, we attempt to estimate the (γ, n) and (γ, 2n) cross sections as a function of photon energy and hence, the total cross section below the (γ, 3n) threshold, for Sb and Ta.

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44 R. Sher, et al., Phys. Rev. 84, 387 (1951).

45 J. A. Harvey, Phys. Rev. 81, 353 (1951).

The reason for limiting ourselves to these two elements will appear shortly.

The shape of the (γ, n) cross section for Ta^{173} (the only isotope of Ta) is known from the work of Johns, et al.[15], but the absolute magnitude is not. Naturally occuring Sb consists of two isotopes, Sb^{121} (56%) and Sb^{123} (44%). The (γ, n) cross section for Sb^{123} has been measured by Johns, et al.[14]. The shape of the (γ, n) cross section in Sb^{121} for those reactions in which the nucleus is left in the 16.4 minute isomeric state, has also been measured. The shape of this cross section curve is within experimental error the same as that for Sb^{123}. We will assume here that the <u>shape</u> of the (γ, n) reaction in which Sb is left in the ground state is the same as that measured for the reaction in which Sb is left in the isomeric state*. Thus, both isotopes of Sb will be assumed to have the same total cross section shape. It would be very natural, both a priori and in view of the assumed similarity in shape between the cross sections in Sb^{121} and Sb^{123}, to assume further that the magnitudes are the same. We shall not do this here, but instead

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* Evidence for the correctness of this assumption is had from the work of R. Montalbetti and L. Katz, Bulletin of the American Physical Society, Vancouver Meeting, June 25, 1951. These authors have measured the cross section curves for $Mo^{92}(\gamma, n)Mo^{91}$ when Mo^{91} is left both in the ground state and in a 15.5 Min isomeric state. They find a peak for both reactions at 18.7 Mev and also find that above 15.5 Mev the shape of the cross section curves are the same. The cross sections begin to differ below 15.5 Mev, but they are small compared to their peak values in that region. Similar results have been found by R. Sagane (private communication).

shall estimate independently the magnitude of the cross section in Sb^{121}; we shall find that it does come out to be very close to that for Sb^{123}.

We already know something about the total cross section in Sb and Ta, since we know the shape of the (γ, n) cross section and up to the (γ, 2n) threshold this is the total cross section. In the last section, we found that the (γ, n) cross section had a maximum, i.e., was flat just at and below the (γ, 2n) threshold. In view of the correlation we have found between the energy at which the (γ, n) reaction is maximum and the (γ, 2n) threshold, it seems very reasonable to assume that the total cross section is fairly flat just beyond the maximum. Starting from this, we can estimate the total cross section above the (γ, 2n) threshold in more detail using the data of Price and Kerst[8] on neutron yields with 18 and 22 Mev bremsstrahlung and the data of McDaniel, et al.[14] on neutron yields with γ-rays from the Li^7(p, γ) reaction.

Price and Kerst have made measurements of the neutron yields from a large number of elements, using 18 and 22 Mev bremsstrahlung. The ratio of these yields is a smoothly varying function of Z for Z greater than about 30. The difference in yields between the 18 and 22 Mev experiments is due to the difference in the bremsstrahlung spectra at these energies, weighted by the cross section (mainly (γ, 2n)). We know what the difference between the 18 and 22 Mev spectra looks like from the work of Schiff[46]. Thus, we can estimate

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[46] L. I. Schiff, Phys. Rev. 83, 252 (1951).

roughly what the (γ, 2n) cross section must be between these energies to agree with Kerst and Price's experiment. This first estimate is rather ambiguous, since there is, of course, more than one shape which will give agreement, but is is a starting point and we shall see later how it can be made more accurate.

Now, using our guess of the shape of the (γ, 2n) cross section we can estimate the absolute cross sections in a way which is insensitive to errors in the (γ, 2n) cross section. Price and Kerst have also measured the relative neutron yields of various elements at 18 Mev, among them Cu. Now, the (γ, n) cross sections for Cu^{63} and Cu^{65} are quite well known. The integrated cross section for Cu^{63} has been measured by three different observers[11,14,32] with fairly good agreement among the three measurements. The measurements of the Cu^{63} cross section by Diven and Almy[11] and by Johns, et al.[15] agree quite well with each other. The cross section curve for Cu^{65} has been measured only by Johns, et al., but it agrees very well with the Cu^{63} : Cu^{65} cross section ratio measurements at 17.5 Mev of Hirzel and Waffler. Thus, there is reason to have considerable confidence in an average of the different sets of measurements on Cu^{63} and of Johns' measurements on Cu^{65}. Then, using the 18 Mev-bremsstrahlung spectrum due to Schiff, we can calculate the absolute neutron yield to be expected from natural copper. Using the relative cross section shapes as estimated above for the element considered, we can also calculate what the absolute magnitude must be to agree with Kerst's 18 Mev data on the yield relative to Cu.

To successfully carry out the analysis outlined above, we must know the shape of the (γ, n) cross section. This is known for all the isotopes in Table II. But now we see why the only elements we can use are Sb and Ta and not Ag and Cu. This is because Kerst and Price use natural isotopic mixtures of the elements and Ag^{109} and Cu^{65} represent only 48.1% and 29.9% of the natural isotopic mixture respectively. On the other hand Ta^{181}, and Sb^{121} and Sb^{123} together, account for approximately 100% of the isotopic abundance of Ta and Sb.

Our estimate of the absolute magnitude of the (γ, n) cross section is insensitive to the estimated shape of the (γ, 2n) cross sections, since most of the neutron yield with 18 Mev bremsstrahlung from Sb and Ta comes from the (γ, n) reaction.

We can check and refine the above rough estimates using other experimental data. McDaniel, et al.[14] have measured the neutron yield relative to Cu from various elements irradiated with the γ-rays from the Li^{7}(p, γ) reaction. These γ-rays comprise a sharp line at 17.6 Mev and another component of about half the intensity with a half-width of about 2 Mev centered at 14.8 Mev. Since we know the cross sections for Cu, and have an estimate of the cross sections for other elements, we can calculate the relative yields to be expected in the experiment of McDaniel and if necessary, correct our previous estimates. The relative yields in McDaniel's experiment are particularly sensitive to the absolute value of the (γ, 2n) cross section at 17.6 Mev. Our results are given in Figs. 1.

The curves in this figure are such as to agree within a few percent with the experimental data we have used to check them, namely the ratio of neutrons yields to that of Cu in the experiments of Kerst and Price, and of McDaniel and the ratio of the 18 and 22 Mev yields in the Kerst and Price experiment. We estimate that they are not in error by more than 15%. Although we have drawn in the total cross section up to 22 Mev, the data does not really tell much about the cross sections above 20 Mev. Thus, as far as this data goes, it is quite possible that above 20 Mev the cross section curve for Sb does not drop off as sharply as indicated, i.e., that there may be a long flat tail which contributes appreciably to the integrated cross sections. For Ta, the situation is quite different. Here the cross section has dropped to less than one-fifth of its maximum value by 20 Mev, hence it seems very unlikely that there is appreciable contribution to the integrated cross section from energies above 22 Mev.

The integrated cross section for the (γ, n) reaction up to 22 Mev in Sb is given by our estimates as 1.82 Mev-barns, which is very close to the value of 2.0 Mev-barns found by Katz for Sb^{123}. This is very reasonable, as we have discussed earlier, in the light of the similarity in cross section shape between Sb^{121} and Sb^{123}.

V. Yields with 330-Mev Bremsstrahlung. Evidence for an Increase in the Total Cross Section at High Energies.

Terwilliger, et al.[30], and Kerst[9] have measured the absolute yields of neutrons using bremsstrahlung with a 330 Mev maximum energy. We can calculate the yields to be expected in Sb and Ta from the (γ, n) and (γ, 2n) reactions by photons of energy up to 22 Mev by using the results given in Fig. 1 for the shape and absolute magnitude of the cross section curves. The formula for the yields with 330 Mev bremsstrahlung is:

$$\text{Yield} \left(\frac{\text{neutrons}}{\text{erg x mole/cm}^2}\right) = 1.77 \times 10^3 \int \left[\left(\sigma_{\gamma,n}(W) + 2\sigma_{\gamma,2n}(W) \quad \ldots\right)\right] \frac{dW}{W}$$

for cross sections in barns. Computing from this formula, one gets for the yields up to 22 Mev of Ta^{181} and the natural isotopic mixture of Sb, 526 and 320 $\frac{\text{neutrons}}{\text{erg x mole/cm}^2}$, respectively. The measured yields* are 940 and 552 $\frac{\text{neutrons}}{\text{erg x mole/cm}^2}$, and are thus higher than the calculated yields by almost a factor two. Thus, there is evidence that a considerable fraction of the neutron yield in experiments with 330 Mev bremsstrahlung comes from photons with energy greater than 22 Mev. A priori, there is no way to decide whether the photon absorption cross section drops off fairly quickly beyond the maximum or whether there is an appreciable tail.

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* The values of Kerst are 27% lower than those of Terwilliger. We have taken as the measured value the arithmetic mean of Terwilliger's and Kerst's values.

For Sb, as we have seen, one cannot say with any certainty whether such a tail exists or not. For Ta, the situation is different. Here, our reconstruction of the cross section curves indicates that the total cross section is small at 22 Mev, and that there is no evidence for an appreciable tail. Moreover, for Pb there is other evidence that shows much more strongly that the extra neutrons which are needed above 22 Mev to give agreement with the 330 Mev data come not from a long tail to the photon absorption cross section, but rather from an increase in the neutron yield for photon energies of the order of 200 Mev.

This evidence is as follows. Terwilliger, et al. have measured the transition curve for the neutron yield in Pb due to 330 Mev photons, i.e., the curve of yield per unit thickness vs. thickness in Pb. This curve is reproduced in Fig. II. Now, we would expect the photon absorption cross section for Pb to be quite similar to that for Ta, except that the maximum should be shifted to a somewhat lower energy, say 14 Mev. But we have a good idea of what a transition curve due to a spectrum of photons with maximum energy around 14 Mev should look like. Such a transition curve is essentially determined by the energy in the photon absorption cross section for which the cross section is a maximum. Its main features do not depend on whether the cross section has a tail or not, provided it is not very large. Strauch[21] has measured transition curves for photon spectra with peaks at 16 and 19 Mev (the (γ, n) cross sections in Ag^{109} and Cu^{63}, respectively). These curves,

normalized to unity at the origin, do not differ by more than 30% at most and usually by much less than that. One can then quite reliably extrapolate them to find the transition curve due to a photon spectrum with 14 Mev maximum energy. This extrapolated curve is shown in Fig. 2, as curve II, normalized to Terwilliger's curve at radiative units. We see that for thicknesses greater than a radiation length, this curve has the same shape within the experimental error as the transition curve in Pb measured by Terwilliger, et al. If we subtract the two we get the transition curve for neutron yield from those photons which are not contained in the spectrum around 14 Mev. The subtracted curve is given by curve III of Fig. 2. We see that it falls off very sharply and thus corresponds to a very high energy. We estimate this energy to be of the order of 200 Mev. The obvious explanation of the source of this high energy yield of neutrons is from the stars produced by mesons, either real or virtual.

The relative contribution to the neutron yield due to the high energy photons as compared with those around 14 Mev in the Terwilliger, et al. experiments is given approximately by the relative height of the two transition curves at $t = 0$, since in these experiments the thickness of the targets was small compared with a radiation length. From the relative heights at $t = 0$, we conclude that for Pb the high-energy photon component contributes about 40% of the neutron yield and the low energy component about 60%. This is in excellent agreement with our results for Ta, where we concluded that the high energy component contributed 44% of the neutron yield.

If we make the guess indicated by the dotted line in Fig. 1 for the cross section of Sb above 22 Mev, we find that this cross section gives an absolute yield of 328 $\frac{\text{neutrons}}{\text{erg x mole/cm}^2}$. This is 59% of the yield found by Terwilliger, et al. Thus, for this estimate of the Sb cross section, 41% of the yield comes from high energy photons.

Finally, our hypothesis that the photon absorption cross section for heavy elements drops off quite sharply beyond the maximum, is supported by direct experimental evidence. Anderson and Duffield[47] have measured the total absorption cross section of U^{238} and find that at 23 Mev. the cross section is a small fraction of its value at 15 Mev, the energy at which the maximum cross section occurs.

VI. Evaluation of $\int \sigma_{total} dW$. Comparison with Levinger-Bethe Formula.

In this section, we try to evaluate the total integrated cross section for photon absorption from experimental data. When this is done we can use this value in Eq. (1) to try to find the fraction of exchange force x in the n-p interaction. The total cross section for photon absorption is the sum of the cross sections for all processes in which a photon is absorbed and a particle (or photon) is emitted. There is sufficient data for the elements $_{30}Zn^{64}$ and $_{73}Ta^{181}$ to evaluate the total cross section with reasonable accuracy. Also, one can get a lower limit from the data on Sb. First, we present our data in Tables III, IV, V and then, discuss the data briefly.

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[47] Roger E. Anderson and Robert B. Duffield, Bulletin of the American Physical Society, Programme of the Chicago Meeting, October 24, 1951.

Table III. Evaluation of $\int \sigma_{total} dW$ and x , the fraction of exchange force in the neutron-proton interaction, for $^{30}Zn^{64}$.

Reaction	$\int \sigma dW$ (Mev-barns)	Source
(γ,n)	.730	Arithmetic mean of the values in references 21, 25, and 36.
(γ,p)	.14	Estimated from evaporation model.
$(\gamma,2n)$	.047	Reference 21.
$(\gamma,2p)$	~ 0	Reference 4.
(γ,pn)	.260	Reference 21.
$(\gamma,p2n)$	$\sim$.12	From values in reference 21 for $^{30}Zn^{66}$, multiplied by two to take account of the fact that $\int \sigma_{\gamma,pn} dW$ for $^{30}Zn^{64}$ is twice that for $^{30}Zn^{66}$.
$(\gamma,p3n)$	$\sim$.066	
$(\gamma,p4n)$	$\sim$.028	

$$\int \sigma_{total} dW = 1.39 \qquad x = .56$$

Table IV. Evaluation of $\int_0^{22} \sigma_{total} dW$ and x , the fraction of exchange force in the neutron-proton interaction, for Sb.

Reaction	$\int \sigma dW$ (Mev-barns)	Source
(γ, n)	1.82	Section II and III.
$(\gamma, 2n)$	.59	Section II and III.
$(\gamma, n > 2)$	?	
$\int_0^{22} \sigma_{total} dW > 2.41$		$x > .44$

Table V. Evaluation of $\int \sigma_{total} dW$ and x , the fraction of exchange force in the neutron-proton interaction, for $^{73}Ta^{181}$.

Reaction	$\int \sigma dW$ (Mev-barns)	Source
(γ, n)	2.96	Section II and III.
$(\gamma, 2n)$	.81	Section II and III.
$(\gamma, n>2)$	~ 0	" " "
$\int \sigma_{total} dW = 3.77$		$x = .56$

We consider first, the data for $^{30}Zn^{64}$ given in Table III. There are several reactions listed, the source of which is the work of Strauch, Reference 21. Strauch has measured only values of the integrated cross sections relative to that of Cu^{63}. To obtain absolute values from his data, we have combined his relative measurements with three measurements of the integrated cross sections for the (γ, n) reaction on Cu^{63} by Johns, et al., Marshall, and Diven and Almy. These authors give this integrated cross section as 0.70, 0.77 $\pm$ .15 and 0.60 Mev-barns, respectively. We have used the mean of these three values, 0.69 Mev-barns, to get absolute values from Strauch's relative measurements.

The integrated cross section for the (γ, p) reaction is obtained from the known (γ, n) cross section combined with the calculations of Weisskopf and Ewing on the relative probability of evaporation of a proton or neutron. This should give a fairly reliable estimate, since the proton is bound much less tightly than the neutron. As we have discussed in the Introduction, in such a case the evaporation theory probably predicts the relative numbers of neutrons and protons fairly accurately. Our calculation neglects the protons which are emitted below the threshold for neutron production, but it is very likely that the number of such protons is small. We would expect the integrated (γ, 2p) cross section to be very small, since the integrated (γ, p) cross section is small. There is also evidence for this from the data of Perlman[4] on the neighboring element Cu^{63}. Perlman finds that the relative yields

for the Cu^{63} (γ, n) and Cu^{63}(γ, 2p) reactions from 50 Mev-bremsstrahlung are 35 and .16, respectively. Assuming that the energy at which the (γ, 2p) cross section is a maximum is about twice that for the (γ, n) gives the result that the integrated (γ, 2p) cross section is about 1% of the integrated (γ, n) cross section. We would expect a similar result from Zn. Also, we would expect that the cross sections for higher order reactions involving two protons as (γ, 2pn), (γ, 2p 2n), etc., are small, as well as the (γ, γ) and (γ, α) reaction. Thus, it is likely that the data listed in Table III includes all reactions whose integrated cross sections are appreciable and that the value for $\int \sigma_{total} dW$ is fairly accurate. Putting this value into the formula (1) gives a value $x = .56$ for the fraction of the exchange force in the n-p interaction. This is in good agreement with the ratio postulated by Serber to explain the high energy n-p scattering. In Tables IV and V, we present data for the evaluation of $\int \sigma_{total} dW$ for Sb and $^{73}Ta^{181}$. As we have noted before, the cross section for Sb is not known above 22 Mev. Hence, the integrated cross section given must be considered to be a lower limit. For Ta, on the other hand, we expect the integrated cross to be, to a good approximation, the sum of the (γ, n) and (γ, 2n) integrated cross sections. Comparing the total integrated cross sections with formula (1), one gets the values of x shown. Considering the errors involved in their calculation, the three

values of x deduced here must be considered to be in good agreement with one another. In these calculations we have had to neglect contributions to the electric-dipole photo-effect from photons with energy greater than 330 Mev, but we expect this to be a very small contribution.

Katz and Penfold[18] have made similar calculations to that of this section for S^{32} and conclude that the integrated cross section is much less, about 1/8 of that expected from the Levinger-Bethe formula. We think the reason for this disagreement is that among other things, they neglect to include the cross sections for higher order reactions in which two or more neutrons are produced. The evidence for this is as follows. We have taken their estimate for the (γ, n) cross section and their measurements of the (γ, pn) cross section and calculated the yield of neutrons to be expected in Jarmie, Jones, and Terwilliger's experiments. The yield comes out to be too low by a factor five. Thus, there seems to be an appreciable cross section from reactions which Katz and Penfold have not taken into account. Of course, this yield might come from neutrons produced by high energy photons in a similar process to the one we had to postulate above to explain the Terwilliger transition curve. In this case the high energy process would have to account for 80% of the neutrons observed with 330 Mev-bremsstrahlung. This seems rather high. If we assume arbitrarily, that as for heavy elements the high energy process accounts for

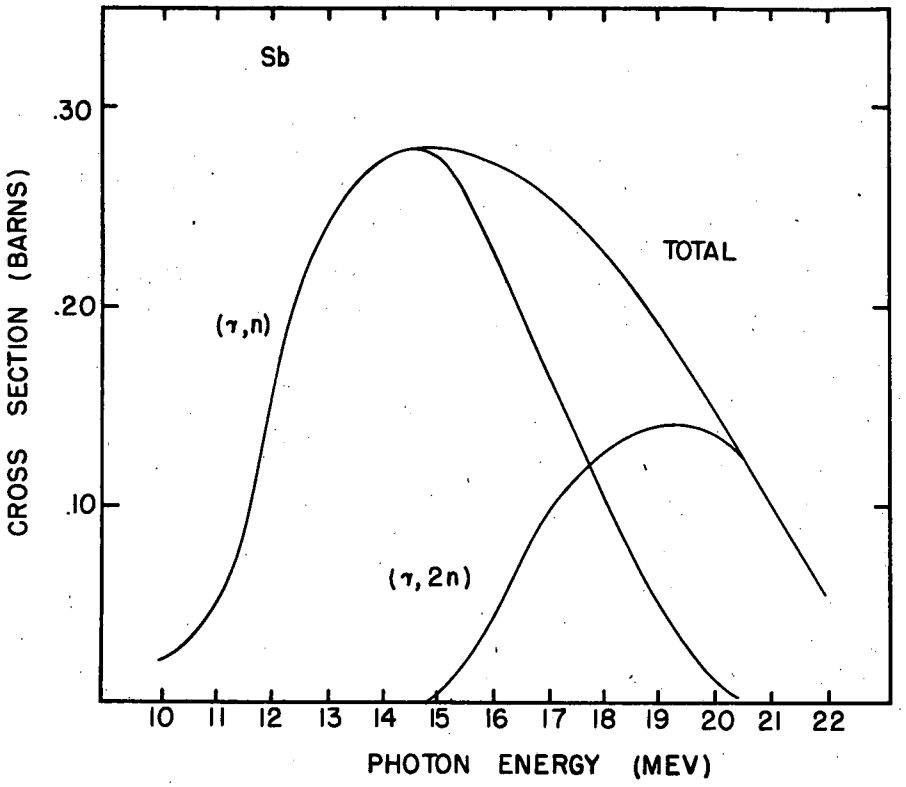
about 40% of the neutron yield, then the (γ, n) cross section alone is too small by a factor three to secure agreement with Terwilliger's results. Thus, the estimate of the (γ, n) cross section is either much too low or else there are higher order reactions with integrated cross sections comparable to that for the (γ, n) process. At any rate, it seems that it would be premature to claim disagreement with the Levinger-Bethe formula until more measurements are made.

This work was performed under the auspices of the Atomic Energy Commission.

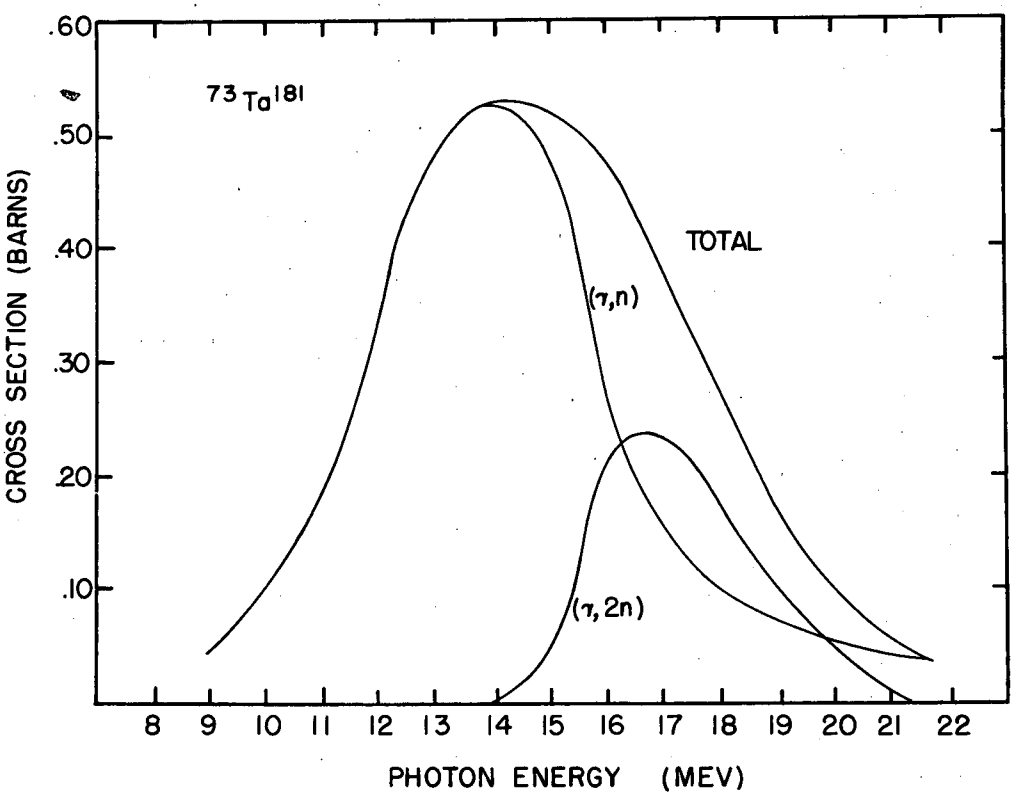
FIGURE CAPTION

Figure 1. Estimate of the (γ, n) and (γ, 2n) cross sections in Sb : (56% Sb^{121} + 44% Sb^{123}) and $^{73}Ta^{181}$. The shape of the (γ, n) cross section is assumed known from the work of Johns, et al. The shape of the total cross section (and hence of the (γ, 2n) cross section) is estimated roughly from Price and Kerst's data on the ratio of neutron yields with 18 and 22 Mev bremsstrahlung. The absolute magnitude of the cross sections can then be found by using the known cross sections in Cu and comparing Price and Kerst's yield at 18 Mev for the element concerned with that for Cu. This estimate is insensitive to errors in the shape (γ, 2n) cross section. Finally, the procedure is checked and refined by using the data of McDaniel, et al. on the yields relative to Cu using γ-rays from the Li(p, γ) reaction. This data is particularly sensitive to the absolute value of the (γ, 2n) cross section at 17.6 Mev.

Figure 2. Decomposition of the transition curve for neutron yield due to 330 Mev-bremsstrahlung in Pb. Curve I is the original transition curve as measured by Terwilliger, et al. Curve II is the transition curve for a spectrum of photons with peak energy at 14 Mev. Curve III is the difference between curves I and II and is presumably the transition curve due to neutrons produced by mesons. It corresponds to an energy of the order 200 Mev.



MU 2780



MU 2781

Fig. 1

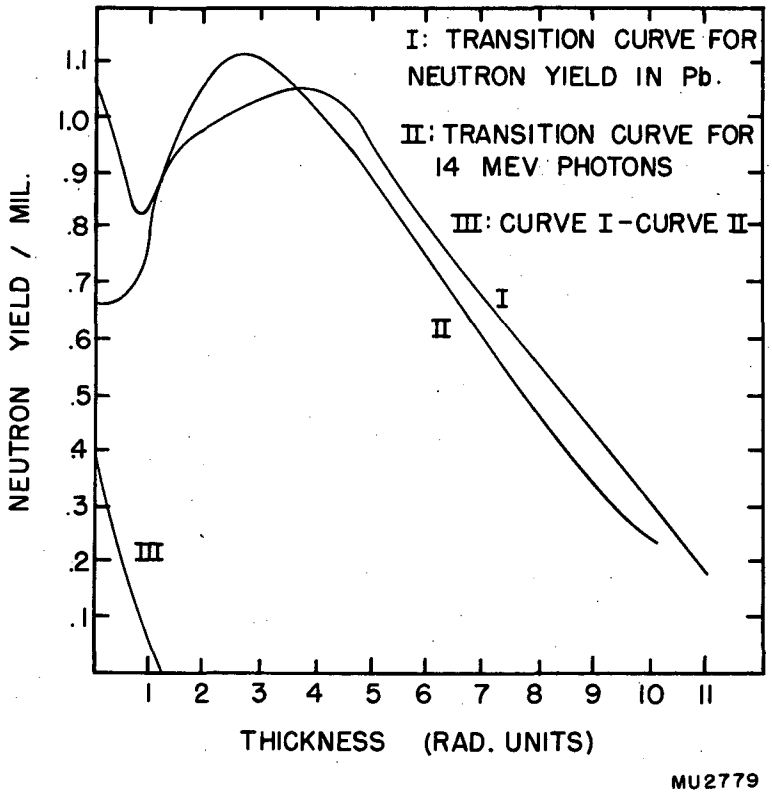

I: TRANSITION CURVE FOR NEUTRON YIELD IN Pb.
II: TRANSITION CURVE FOR 14 MEV PHOTONS
III: CURVE I - CURVE II
NEUTRON YIELD / MIL.
1.1
1.0
.9
.8
.7
.6
.5
.4
.3
.2
.1
I
II
III
1 2 3 4 5 6 7 8 9 10 11
THICKNESS (RAD. UNITS)
MU2779

Fig. 2