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BEAM FOIL SPECTROSCOPY

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IMPROVED RESOLUTION METHODS FOR BEAM FOIL SPECTROSCOPY\*

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Abstract

In general, the resolution that can be achieved by conventional beam foil spectroscopy is limited by the effects of cascading, spread in the beam velocity, beam divergence and uncertainty in the beam velocity. We shall discuss a class of experiments which does not depend on these properties of the ion beams from low energy accelerators. We believe that by proper choice of experimental conditions, extremely high precision can be achieved by the technique of beam foil spectroscopy.

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## 1. Introduction

The most remarkable property of beam foil spectroscopy (BFS), in our opinion, is that the excitation occurs at a well defined time (foil position) in the extremely short time of about  $10^{-5}$  nsec. This property has been used over the past several years to measure mean-lives of excited states of atoms and ions. In the past three years, in collaboration with the beam-foil group at the University of Arizona, we started a program to observe other phenomena such as atomic and ionic alignment with the hope that methods may be found to yield measurements of improved resolution and precision. We believe that the first clue to the possibility of high resolution experiments was the observation that atoms and ions which are excited by the foil are aligned to a sufficiently high degree that experiments based on alignment can be performed<sup>1</sup>). Similar experiments were carried out, in the case of beam-gas collisions by Ray Hughes<sup>2</sup>) and a group under Dufay in Lyon<sup>3</sup>). A theory was developed by Van den Bos<sup>4</sup> for the proton-hydrogen collision. In the case of the electron capture process by protons of high velocity from the hydrogen atom, the theory predicts that the cross section for capture leading to states of lower magnetic quantum number is larger than for capture to higher quantum number states. Here, the axis of quantization is along the beam direction. In other words, the theory predicts that the excited states formed by the electron capture process are aligned along the beam direction for high velocity ions. The experimental results of several investigators have shown that the gross features of the experimental observations agree with the theory. Although the excitation process involved in the case of atoms and ions passing through a foil is much more complicated than beam-gas collisions, the atoms and ions are aligned in a manner very

similar to that of gas collisions. In general, excited states of almost all the atoms and ions formed by beam-foil collisions have been shown to be aligned for those states that are characterized by  $L \geq 1$ ,  $J$  and  $F > 1/2$ . Thus, for the atoms and ions aligned by beam-foil and beam-gas collisions, the technique of Hertzian (or R.F.) spectroscopy, first developed by Brossel and Bitter<sup>5</sup>) in 1952, can be applied. The basic advantage of RF spectroscopy over conventional optical spectroscopy is that the precision of the measurements is not influenced by Doppler broadening. Thus, most high precision measurements have been made by a form of RF spectroscopy. About 10 years after the development by Brossel and Bitter, of RF resonance techniques for excited states of atoms, the non-zero field Hanle Effect (level crossing) technique was developed by Franken<sup>6</sup>). The precision of measurements made by the level-crossing technique is also dependent only on the natural line width and is not affected by Doppler broadening. Remarkable advances in RF spectroscopy took place soon after. These were; light beats by Dodd and Series<sup>7</sup>), anti-level crossing by Wieden and Eck<sup>8</sup>), and many phenomena associated with quantum field theory, developed primarily by Cohen-Tannondji<sup>9</sup>). None of these phenomena can be observed unless the states are either aligned or polarized. Conversely, if atoms or ions are aligned, all of these phenomena are observable, at least in principle.

We have been conducting a systematic study to attempt to apply these techniques developed by RF spectroscopists to beam foil spectroscopy. However, we must understand the basic differences between the two methods. One of the most important is that in the case of RF spectroscopy (including the atomic beam technique), the atoms move at thermal velocities on the order of  $10^5$  cm/sec. On the other hand, in BFS the atoms or ions move at velocities of  $10^8$  cm/sec or higher.

Thus, we must consider the uncertainty principle relation  $\Delta\nu\Delta t \sim 1$ . In the case of RF spectroscopy  $\Delta t$  is the life-time of the state while  $\Delta t(\text{obs})$  for BFS can vary from a fraction of a life-time to several life-times. In BFS, the precision,  $\Delta\nu \sim 1/\Delta t$ , can be varied over a considerable range depending on the experimental conditions. Roughly speaking, if one can set the experimental conditions so that  $\Delta t(\text{obs}) > \tau$  (the mean-life of the state),  $\Delta\nu$  can be below the natural line width. Meeting these experimental requirements is an extremely difficult task in RF spectroscopy while relatively simple in BFS. We shall discuss the basic features of experiments that can achieve high resolution by arranging the experimental condition so that  $\Delta t(\text{obs}) > \tau$ .

## 2. Theory of Improved Resolution by BFS

In general, there are two basic techniques available that should yield high precision measurements; RF resonance and level crossing. By conventional methods, the RF resonance and level crossing phenomena are integrated over a time interval much longer than the mean-lives of the states of interest since atoms involved in the resonance or level crossing remain in the interaction region for a time long compared with the mean-life of the state. Thus, the resonance width is approximately  $\Delta V \sim \frac{1}{\pi\tau}$  where  $\tau$  is the life-time of the excited state.

On the other hand, by BFS, because of the high velocity of the atoms and ions, one can quite readily make an observation at a time longer than the natural life-time. Such a detection method was used by Ma, et al. for an RF resonance experiment<sup>10</sup>) and Copley, Kible, and Series<sup>11</sup> for a level-crossing experiment. Both of these experiments were carried out using a conventional light source (not BFS source). We believe that the technique developed by these investigators is most suitable for BFS.

The experimental condition we are interested in is one in which an ion beam passes through a thin foil resulting in the alignment of excited states of ion or atom. Now, let the beam interact with an oscillating RF field or an appropriate level crossing field, and start the detection at a finite time ( $t$ ) after excitation for a duration  $\Delta t$ .

We shall first describe the time-delayed detection of level-crossing of  ${}^4\text{He}$  in the  $3^3P_{1,2}$  state for  $\Delta M_J = 2$  crossing as shown in fig. 1.

### 3. Theory

The intensity of light emitted by a  $^4\text{He}$  atom in the  $^3\text{P}$  state at time  $t$  after excitation and with polarization vector in the  $y$ - $z$  plane is given by

$$\begin{aligned}
 I(\omega, t) = & A e^{-\gamma t} \{ 1 + a_1 \cos \omega_{12} t + a_2 \cos \omega_{02} t \\
 & + a_3 \cos(2\omega t + 2\theta) + a_4 \cos[(\omega_{12} - 2\omega)t - 2\theta] \\
 & + a_5 \cos[(\omega_{12} + 2\omega)t + 2\theta] + a_6 \cos[(\omega_{02} - 2\omega)t - 2\theta] \\
 & + a_7 \cos[(\omega_{02} + 2\omega)t + 2\theta] \}
 \end{aligned}$$

and the signal observed by a detector with a slit extending from  $\ell_1$  to  $\ell_2$ , is given by  $S(\omega) = \int_{t_1}^{t_2} I(\omega, t) dt$ , where  $\omega_{ij}$  are the fine structure separations,  $\omega = g_J \mu_0 H/t$  and  $\theta$  is the angle which the electric field vector of the light makes with the beam axis as in fig. 2. The coefficients  $a_i$  are determined by the initial state and angular factors from the electric dipole matrix element;  $t_1$  and  $t_2$  are defined by  $t_1 = \ell_1/v$ ,  $t_2 = \ell_2/v$  where  $v$  is the beam velocity.

The atom is assumed to emerge from the foil in an aligned state  $\psi = |L = 1 m_L = 0, S = 1 m_S \rangle$  with respect to the beam direction. In the presence of a magnetic field  $H$  along the  $z$ -axis the state vectors are rotated by  $\pi/2$  so that expanding  $\psi$  in  $Jm$  states we may write

$$\psi(t = 0) = \sum_J \sum_{m_J'} C_{m_J}^{(0)} \mathcal{D}_{m_J', m_J}^{(J)}(0, \pi/2, 0)$$

The time evolution of  $\psi$  is obtained by solving the Schrodinger equation for the coefficients  $C(t)$  from which the intensity fluctuations are derived.

The above result is strictly true only for low magnetic fields where  $\omega \ll \omega_{ij}$ . In the region of our interest  $2\omega \sim \omega_{1,2}$ . Here the eigenfunctions are no longer those of  $J_z$ . The Zeeman interaction mixes the  $m_J$  states and the solution of the Schrodinger equation is very much complicated and must be carried out numerically. If we confine our attention to the region of the two crossings (2,0) and (1,-1) then the signal observed by a detector having a finite slit width can be represented by two terms

$$S(\omega) = \int_{t_1}^{t_2} B e^{-\gamma t} \cos[(\omega' - 2\omega)t - 2\theta] dt \\ + \int_{t_1}^{t_2} C e^{-\gamma t} \cos[(\omega'' - 2\omega)t - 2\theta] dt$$

where  $\omega = (\frac{\partial w}{\partial H})/\hbar$  where  $w$  is the energy,  $t_1$  is the time at which observation begins ( $\ell_1/v$ ), and  $t_2$  the time at which observation ends ( $\ell_2/v$ ). The high frequency components integrate out rapidly and contribute very little to the signal. The constant part of the signal is dropped for simplicity. Figure 1 shows the level crossings in the  $^3P_{1,2}$  states of  $^4\text{He}$ . The integrations are readily performed and in figs. 3-5 the signal is shown as a function of the parameters  $t_1$ ,  $t_2$ ,  $\theta$ , and  $H$ . In these calculations we have taken  $B = C$  and justify this for the present on experimental grounds. Our purpose here is not to fit line shapes but to show in a quantitative way how the signal behaves with the various parameters available to us in beam foil work. By proper selection of  $t_1$  and  $t_2$ , the two crossings, at 161.7 and 166.5 gauss can be picked out with high accuracy as illustrated in fig. 6. Although the modulation in the wings is an appreciable fraction of the

crossing signal they can be distinguished from the crossings by shifting the limits of integration (i.e., shifting the detector aperture up or down stream). In that case the position (and frequency) of the modulation changes but the level crossing peaks do not move.

The expression for RF resonance can be obtained by a similar calculation. The result of the calculation is similar to that for level crossing, again with undulations in the resonance curve.

#### 4. Experiment

Since alignment is quite an important part of the experiment, we shall begin our discussion with the data on alignment. Our first experimental result was that which we performed about two years ago on  ${}^7\text{Li}$  alignment by beam foil and beam-gas electron capture. In the case of foil excitation, we simply observed quantum beats in the field region given by

$$I(H) \propto e^{-\Gamma t} \left[ 1 + A \cos \frac{2g_J \beta H}{\hbar} t \right] .$$

Thus, it is evident that one should observe periodic changes in light intensity as we vary the magnetic field  $H$ , keeping  $t$  constant by observing at a fixed distance  $\ell$  down stream from the foil (since  $t = \frac{\ell}{v}$ ).

Figure 2 shows the experimental arrangement and fig. 7 shows typical experimental results on quantum beats<sup>12</sup>. The polarization ratio  $\pi = (I_{\parallel} - I_{\perp}) / (I_{\parallel} + I_{\perp})$  is approximately 5 to 10% at energies of 20 keV to 70 keV, with alignment increasing with energy. In the case of beam gas collision, the alignment was observed by the Hanle effect<sup>13</sup>) (see fig. 8). In this case, the alignment was 22% which represents complete alignment after taking the hyperfine interaction into account.

After a few experiments on other atoms by the Arizona group, we came to the conclusion that the alignment that takes place by BFS approximately satisfies the proton-hydrogen collision theory, i.e., the cross section for charge capture in  $m_{\ell} = 0$  state is larger than for  $m_{\ell} > 0$ . We have, for the time being, abandoned the experimental study to determine the mechanism for alignment and instead have begun a program to achieve high resolution. The

technique we are currently using is level-crossing since we have not yet constructed an RF field system for resonance work.

We shall compare BFS results with extreme high precision work done by electron impact excitation at LBL by Dr. Edmond Geneux when he visited our laboratory. His results are shown in fig. 9. Figure 10 shows the experimental arrangement for delayed detection of level crossings in <sup>4</sup>He and in fig. 11 we give the results of the first successful experiments. The line widths are still greater than the natural width, but will decrease with increasing integration. Note the undulations as predicted by the theory.

5. Conclusion

We believe that our experimental observations of time delayed level crossing on  $^4\text{He}$  show conclusively the powerful feature of BFS for high precision measurements. In addition to the narrow signal width, an additional advantage of BFS is that the experiment is carried out in a vacuum so that the collision effect from the surrounding atoms that usually takes place in conventional rf spectroscopy is absent, and high field stark effect experiments can also be achieved without the problem of electrical breakdown of gas.

FOOTNOTES AND REFERENCES

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## FIGURE CAPTIONS

Fig. 1. Level system for  ${}^4\text{He}, {}^3\text{P}_{1,2}$ .

Fig. 2. Experimental arrangement for BFS measurements involving alignment by foil or gas collisions.

Fig. 3. Calculated level crossing signal for the  ${}^4\text{He}, {}^3\text{P}_{1,2}$  system, polarization angle of observation =  $0^\circ$

a) delayed  $0.1 \tau$ , integrated over  $0.3 \tau$

b) delayed  $0.1 \tau$ , integrated over  $0.4 \tau$ .

Fig. 4. Calculated level crossing signal for the  ${}^4\text{He}, {}^3\text{P}_{1,2}$  system. Polarization angle of observation =  $45^\circ$  (dispersion signal)

a) delayed  $0.1 \tau$ , integrated over  $0.3 \tau$

b) delayed  $0.1 \tau$ , integrated over  $0.4 \tau$ .

Fig. 5. Calculated level crossing signal for the  ${}^4\text{He}, {}^3\text{P}_{1,2}$  system. No delay, integrated over  $10 \tau$  (approximately the natural line-width)

a) polarization observation angle =  $0^\circ$

b) polarization observation angle =  $45^\circ$  (dispersion signal)

Fig. 6. Calculated level crossing signal for the  ${}^4\text{He}, {}^3\text{P}_{1,2}$  system. Delayed for  $1.0 \tau$ , integrated for  $2\tau$ . Note line width is below natural width, but signals are accompanied by undulations resulting from incomplete integration.

Fig. 7. Light beats in  ${}^7\text{Li}, {}^2\text{P}$  system for different values  $L$  of the distance from the foil.

Fig. 8. Hanle effect in  ${}^7\text{Li}, {}^2\text{P}$ , observed by beam-foil excitation and alignment.

Fig. 9. Electron impact level crossing in  ${}^4\text{He}, {}^3\text{P}_{1,2}$ . Data of E. Geneux.

(a) Lower field crossing, (b) Higher field crossing.

Fig. 10. Experimental arrangement for  ${}^4\text{He}$  level crossing measurements.

Fig. 11. Observed level crossings in  ${}^4\text{He}, {}^3\text{P}_{1,2}$ .

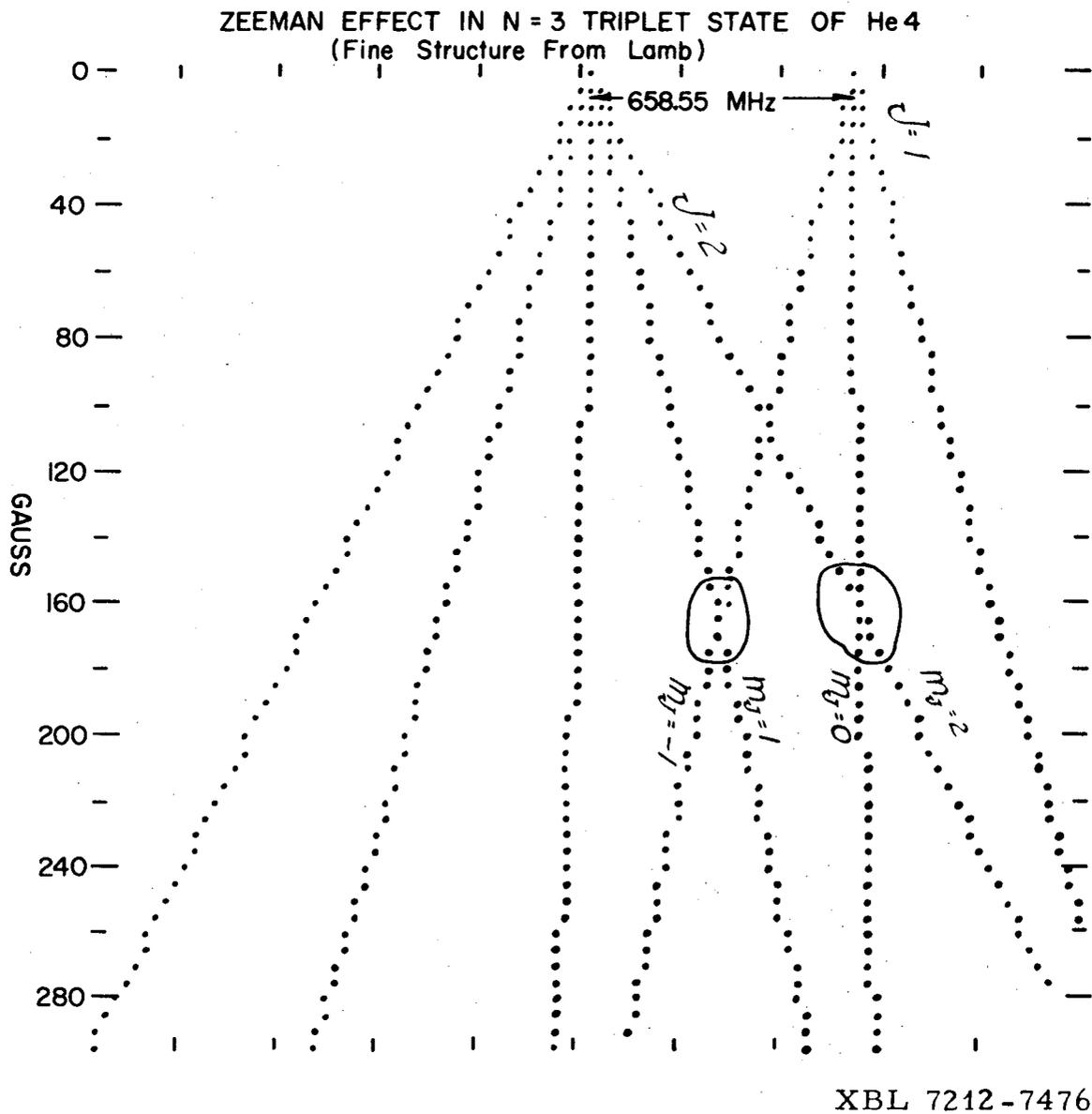
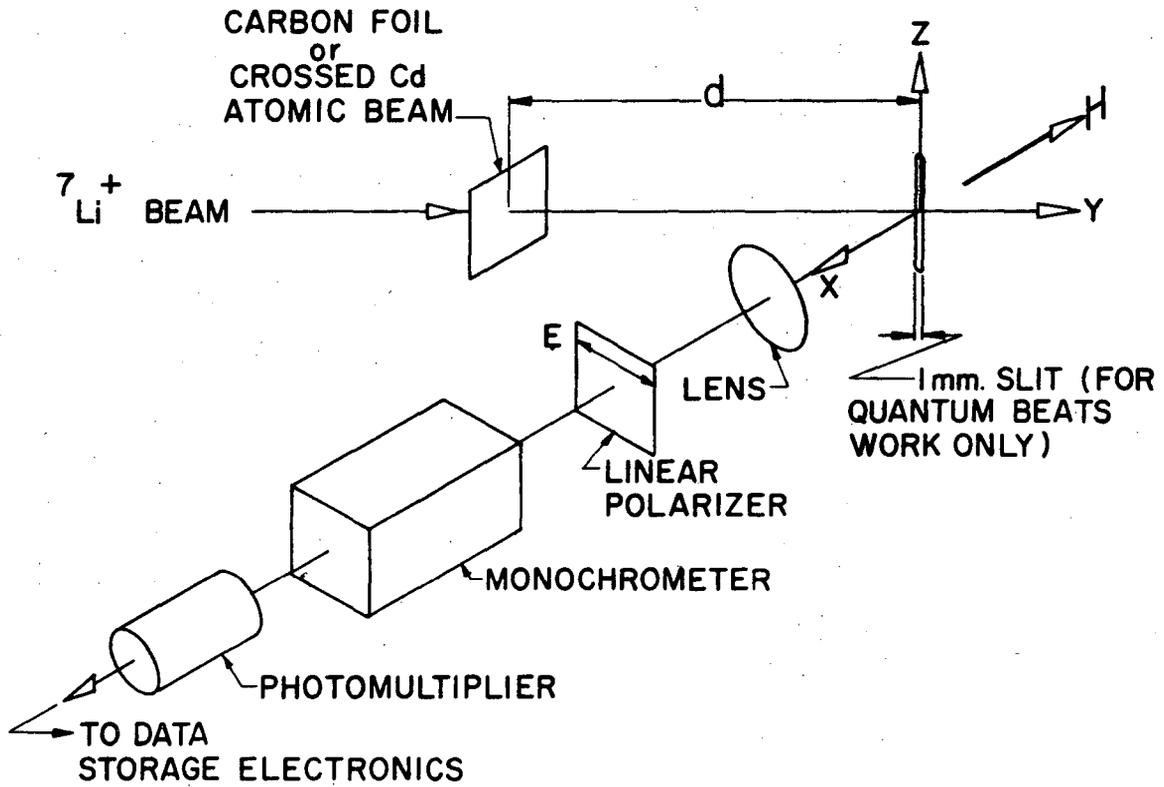


Fig. 1



XBL 713-550

Fig. 2

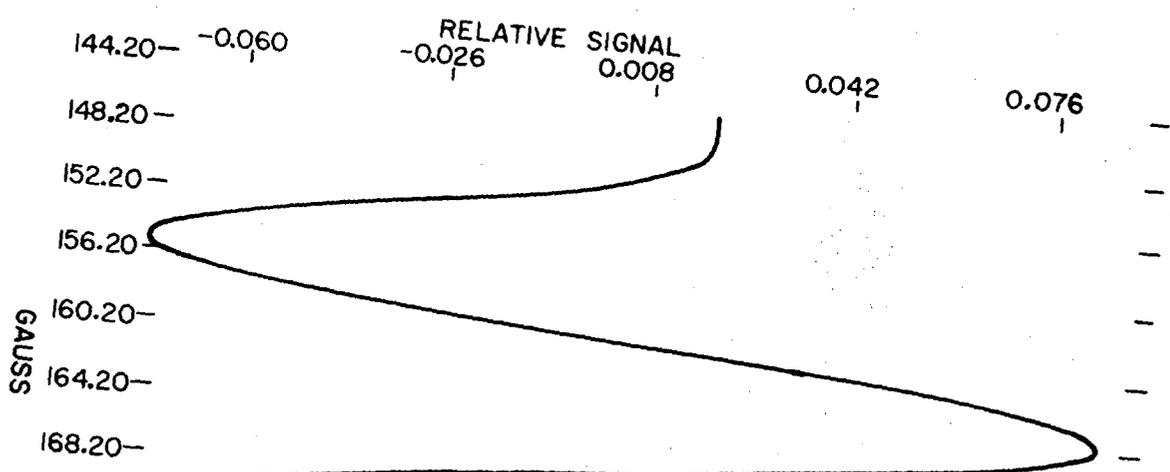


Fig. 3a

Lifetime = 93.00nSec  
 Gamma T<sub>1</sub> = 0.10, Gamma T<sub>2</sub> = 0.30  
 Observation Angle = 0°

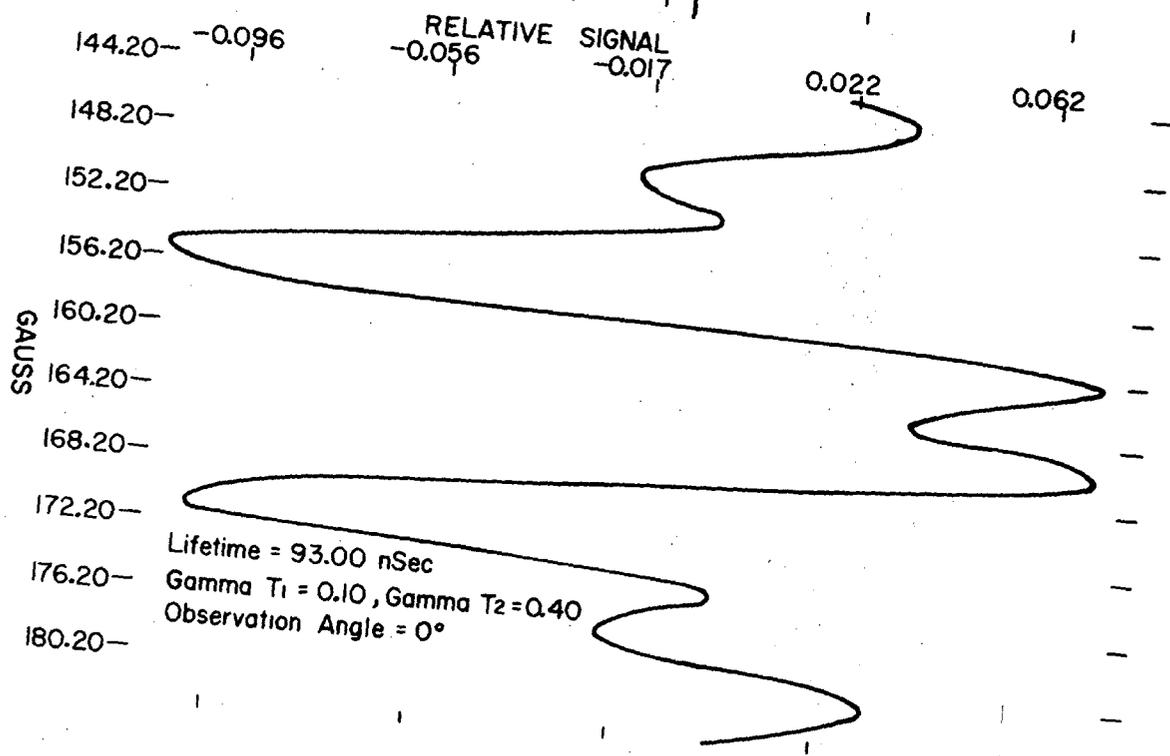


Fig. 3b

Lifetime = 93.00 nSec  
 Gamma T<sub>1</sub> = 0.10, Gamma T<sub>2</sub> = 0.40  
 Observation Angle = 0°

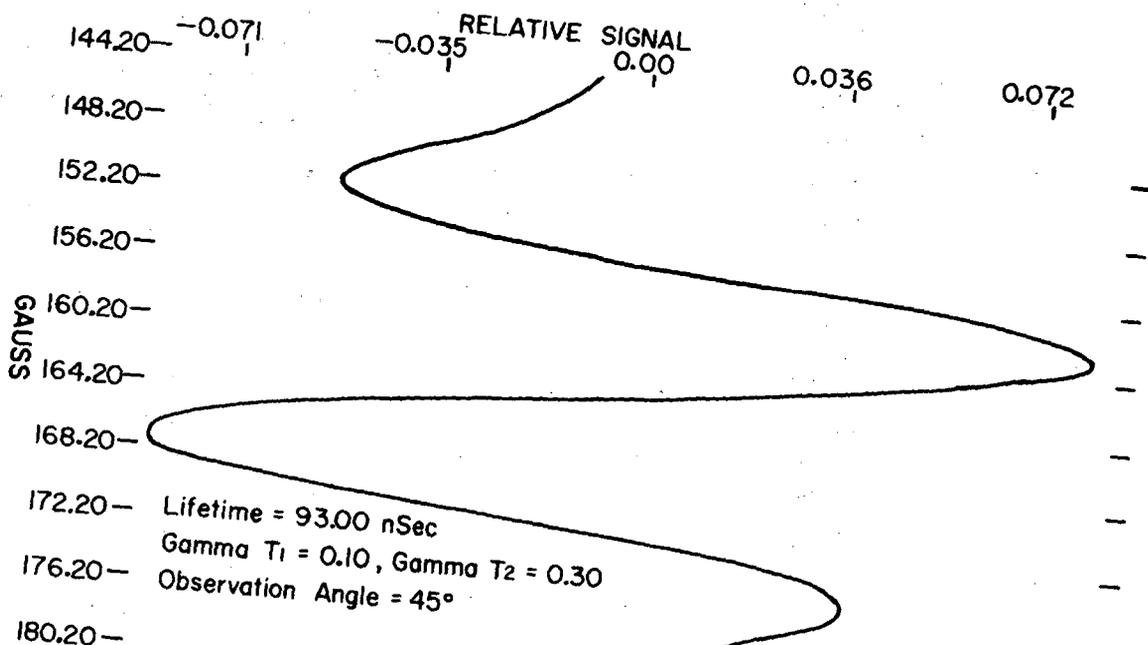


Fig. 4a

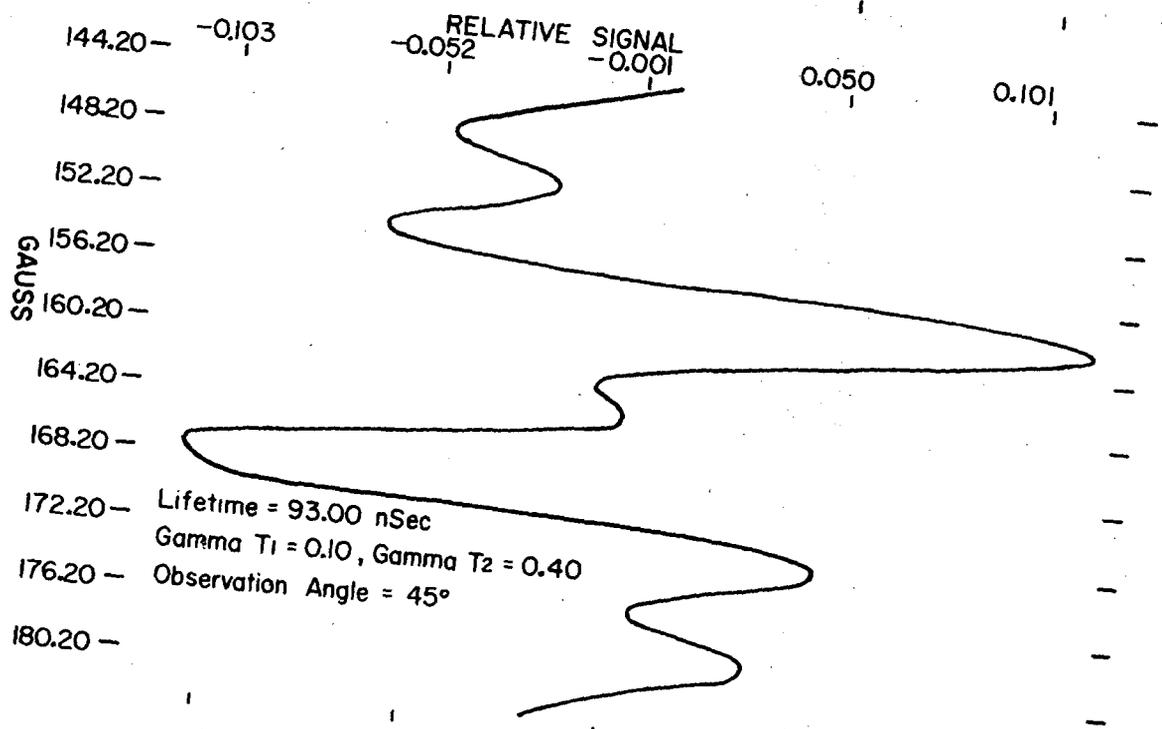


Fig. 4b

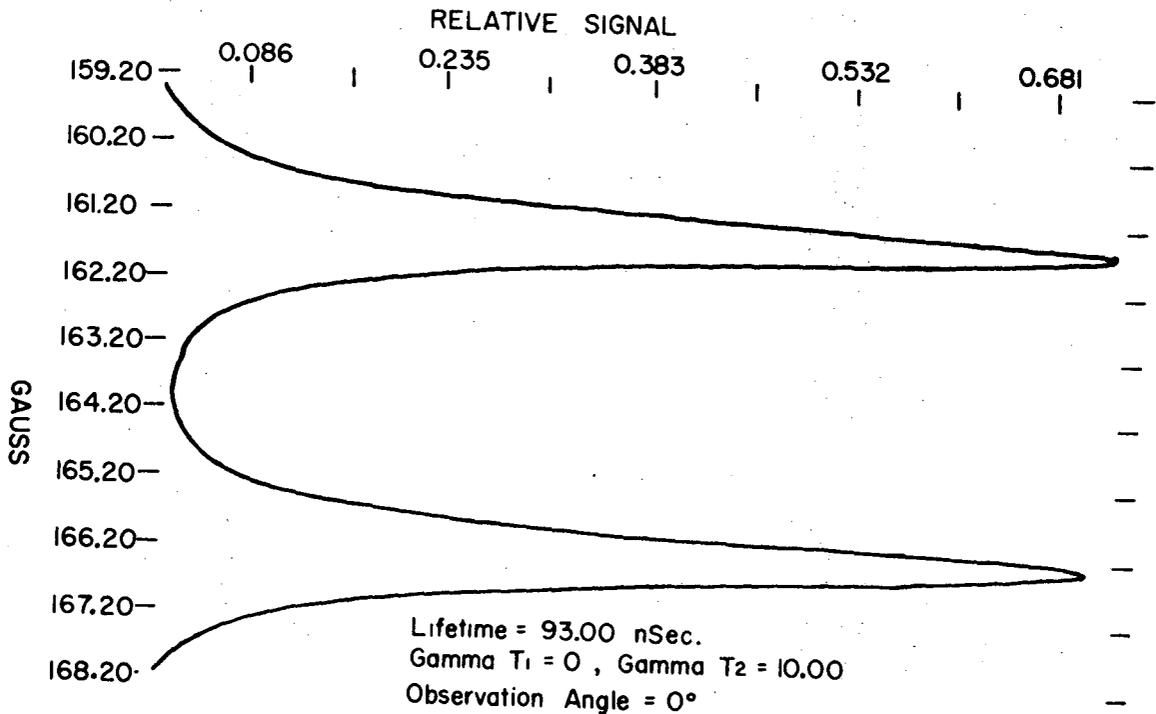


Fig. 5a

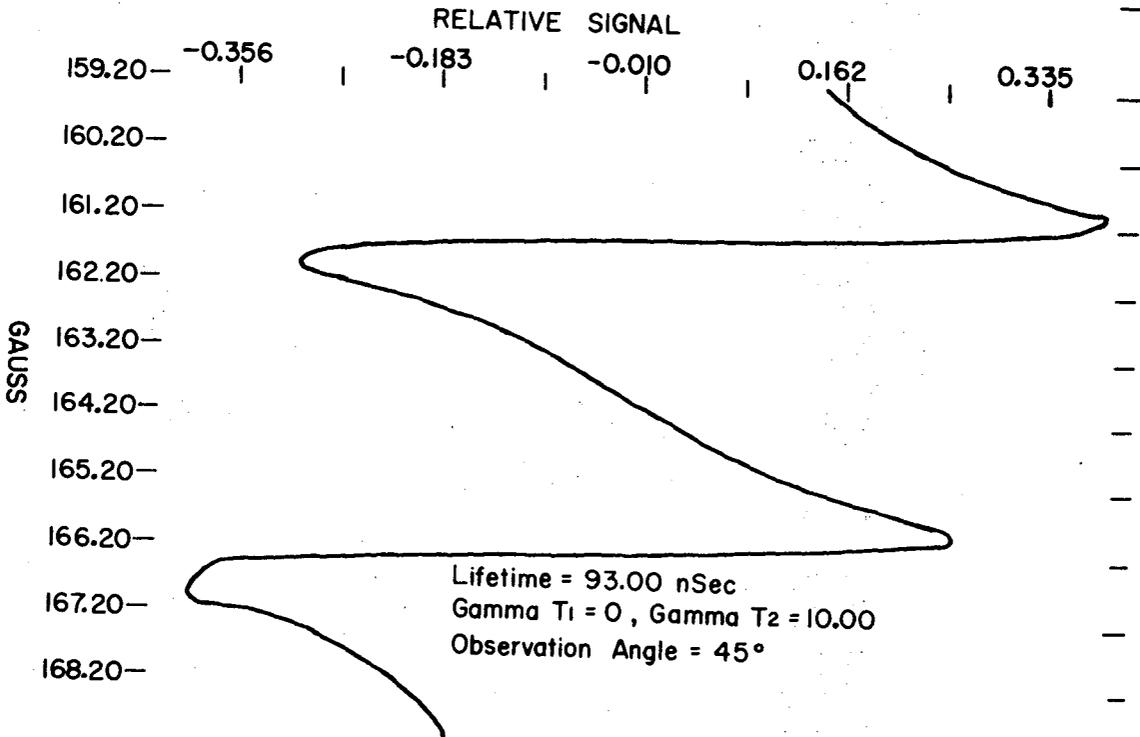
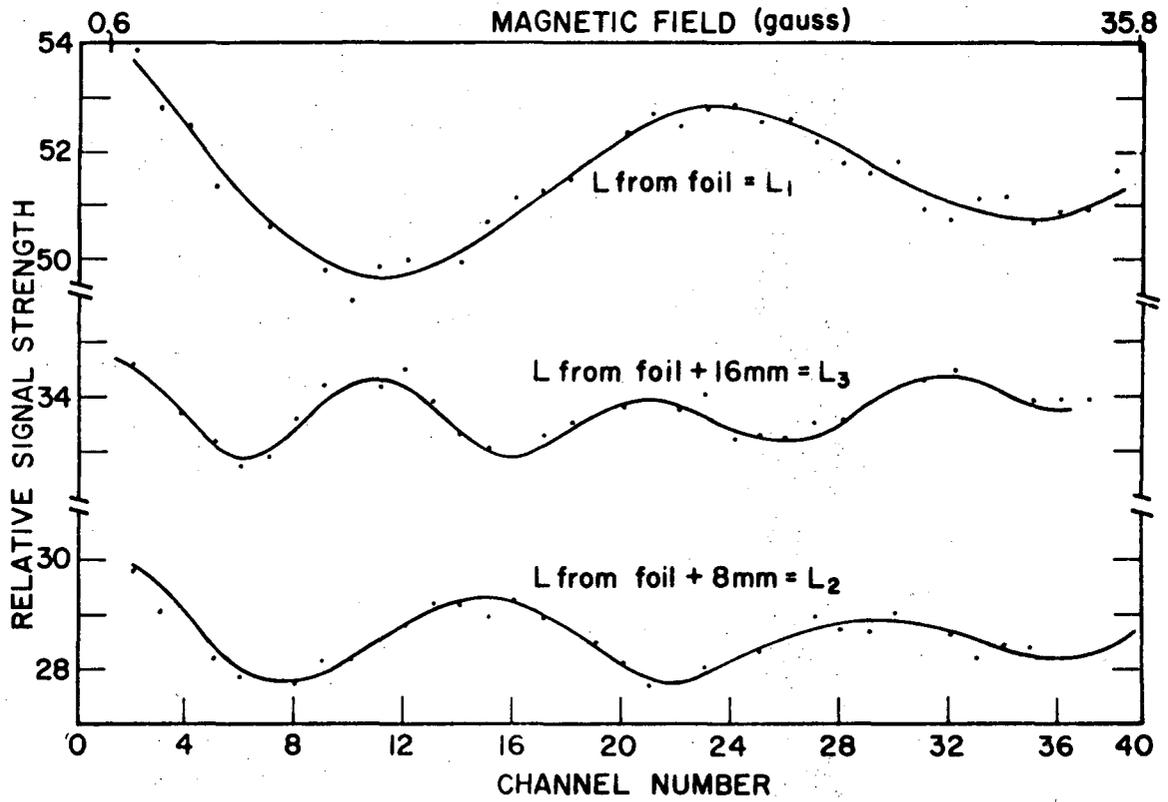


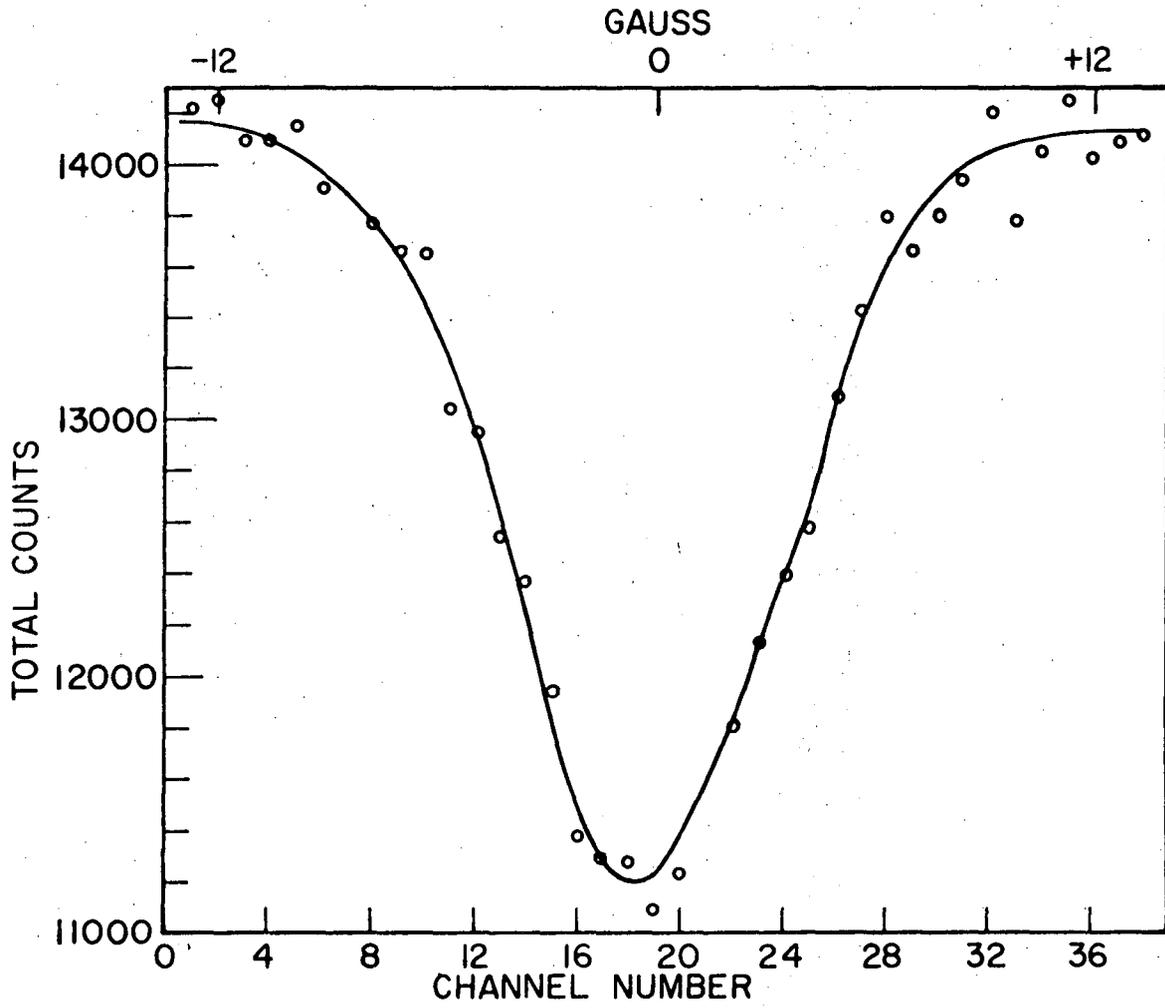
Fig. 5b





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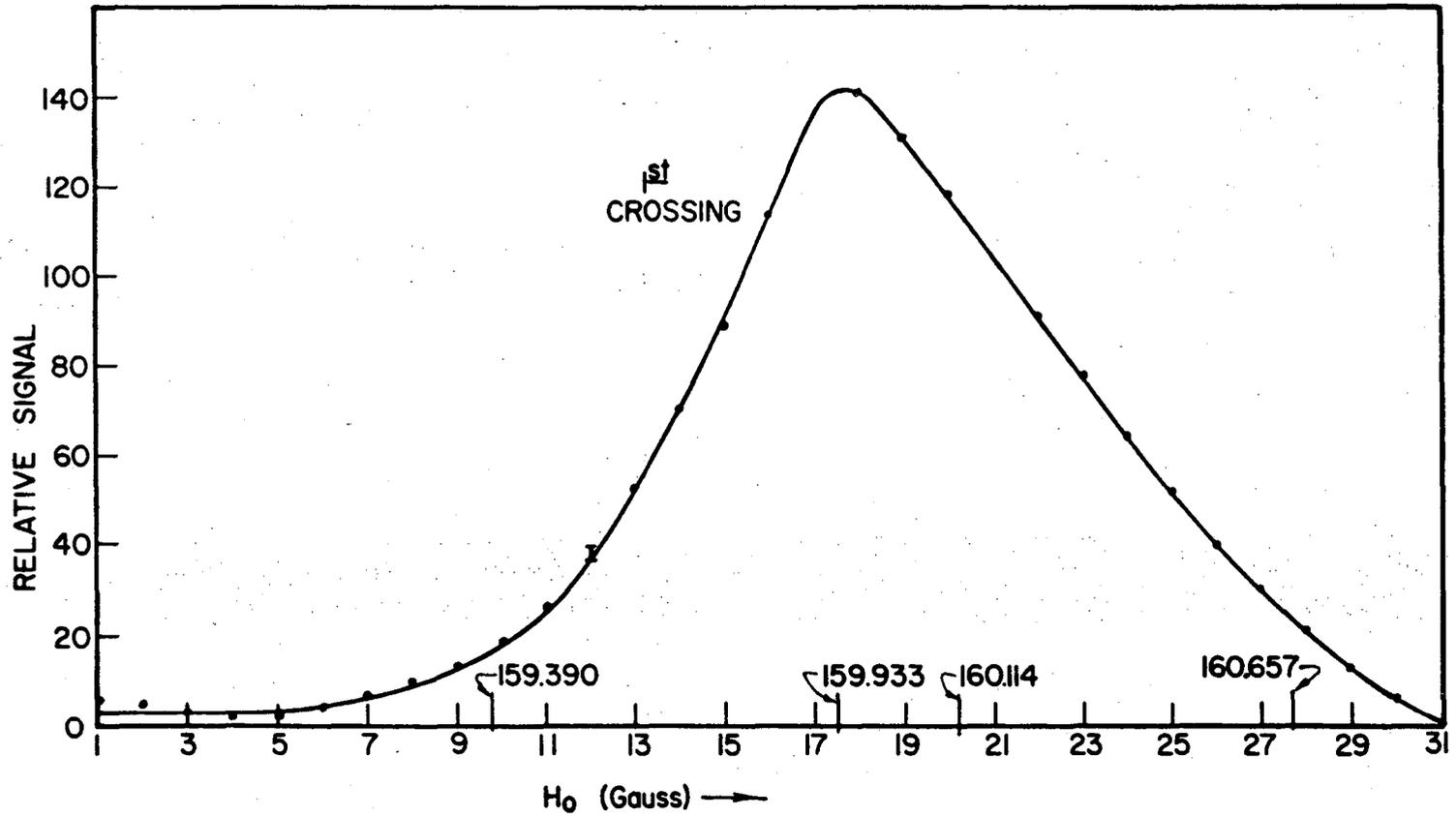
Fig. 7



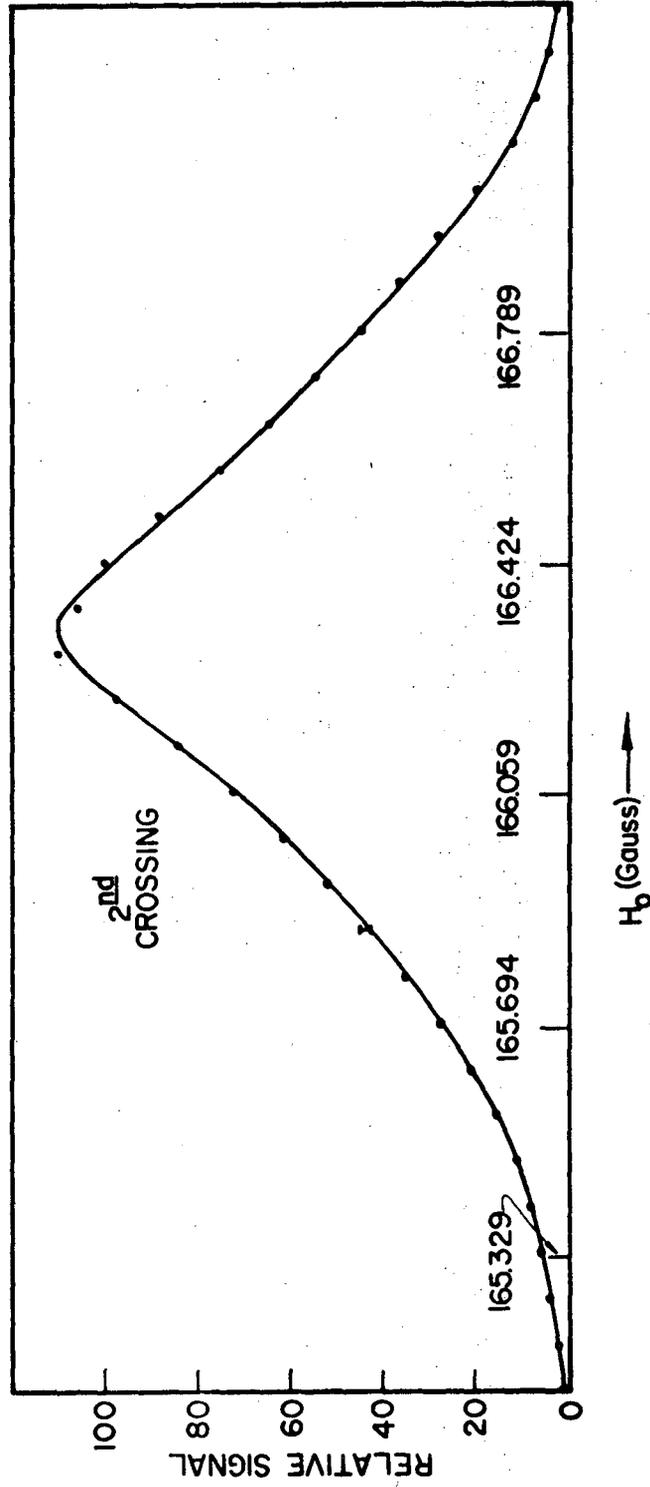
XBL 713-547

Fig. 8

Fig. 9a



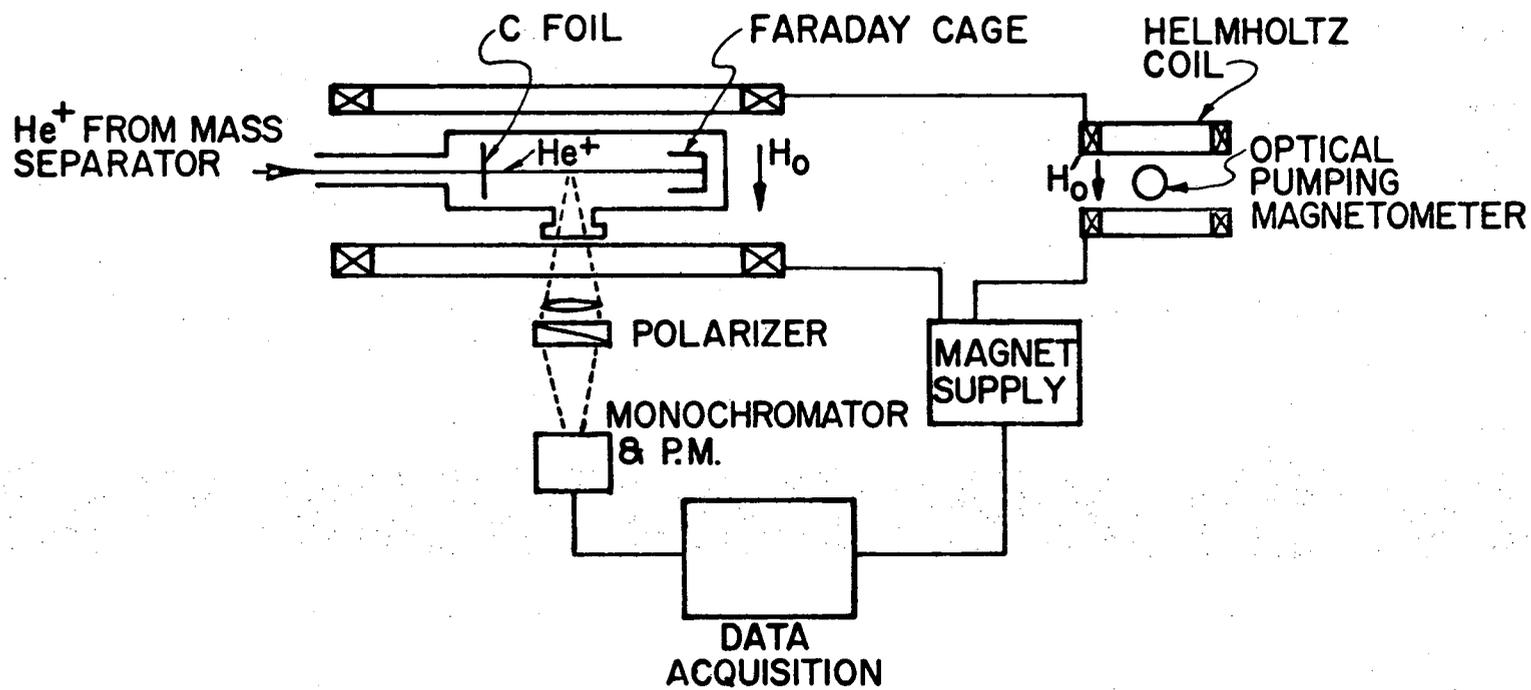
XBL 729-1918



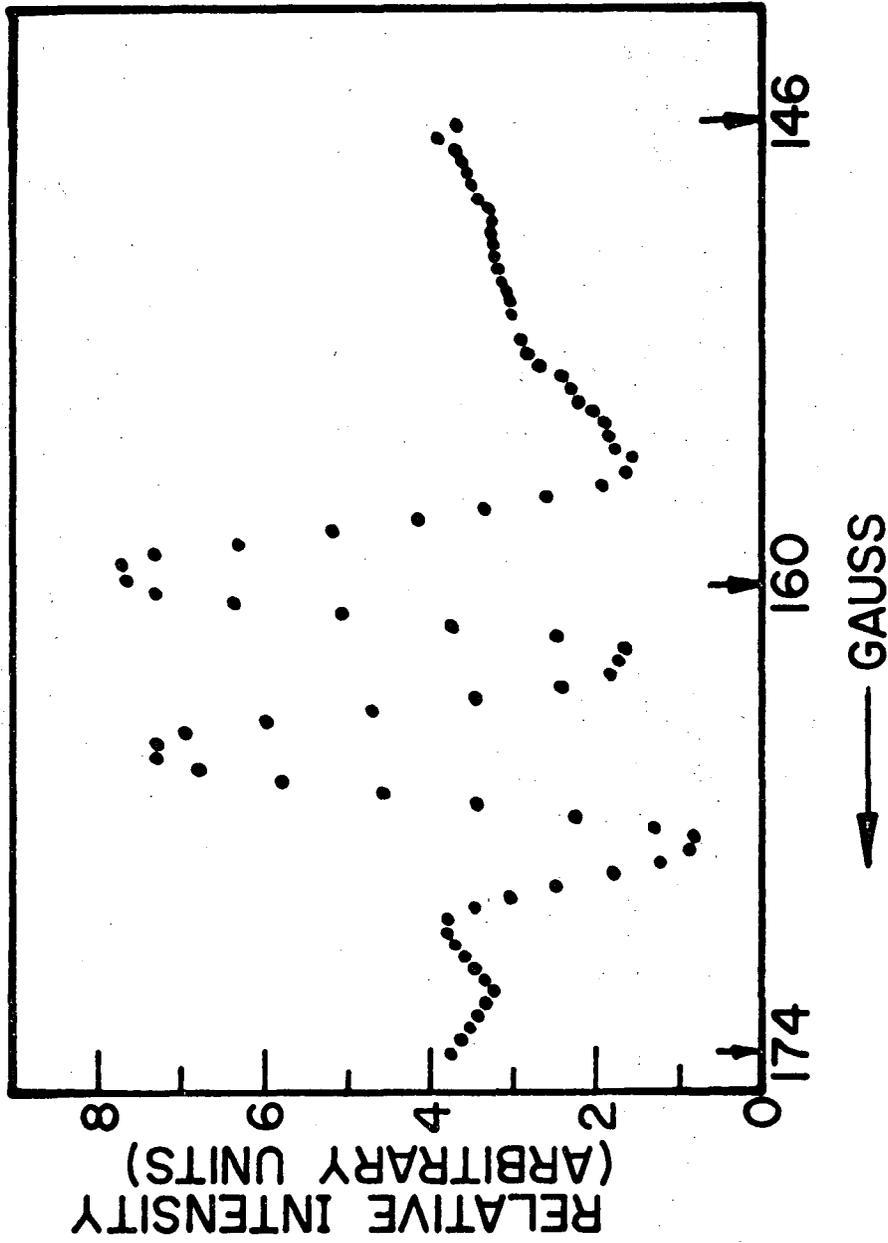
XBL 729-1919

Fig. 9b

FIG. 10



XBL 729-1917



XBL 729-1949

Fig. 11

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